

# Erasing Appearance Preservation in Image Smoothing

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## Supplementary Material

2 In this document, we provide additional details of the model verification, additional  
3 technical backgrounds, additional implementation details, more qualitative results,  
4 more comparisons, raw user study data, and raw experimental data.

5 All involved tests, datasets, methods, results, and statistics are already presented in  
6 the main article, and this document only contains detailed extensions or implemen-  
7 tations.

8 All EAP results in this document are achieved using our knapsack solver in absence  
9 of user interaction.

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Figure 1: Texture dataset with human annotated ground truth pixel-wise texturalness measurement.

## 64 1 Additional Details for Verification

65 In the main article, we have modeled the EAP (Erasing Appearance Preservation) pixel-wise sup-  
 66 porting position selection task as a knapsack problem. Here we detail our verification on [Xu et al.](#)  
 67 [\[2012\]](#)'s dataset as presented in the main paper (*Section 2.1, line 351-354*). Our models in the main  
 68 article are:

69 **Knapsack item value.** For any pixel at position  $p$ , we have modeled item value  $v_p$  as

$$v_p = \sum_{i \in l_p} \sum_{j \in l_p} w_{ij} \|\tau(\mathbf{X}_i) - \tau(\mathbf{Y}_j)\|_2^2 \quad (1)$$

70 where  $l_p$  is a local window surrounding  $p$ ,  $\tau(\cdot)$  is CIE RGB-to-Lab transform, and  $\mathbf{X}$  and  $\mathbf{Y}$  are  
 71 source and smoothed images respectively. Gaussian term  $w_{ij} = \exp(-\|\mathbf{X}_i - \mathbf{Y}_j\|_2^2 / 2\sigma^2)$  makes this  
 72 value faithful to human perception.

73 **Knapsack item weight.** The modeling of item weight  $w_p$  is

$$w_p = \epsilon + \sum_{i \in l_p} \sum_{j \in l_p} \|\mathbf{Y}_i - \mathbf{Y}_j\|_2^2 \quad (2)$$

74 where  $\epsilon$  is a scaler to prevent zero weights. This weight modeling is aimed at protecting desired  
 75 details in images, as mentioned in the main article.

### 76 1.1 Objective

77 The fundamental goal of EAP knapsack is to identify pixel positions with task-specific patterns, *i.e.*,  
 78 discovering textural pixels for texture removal, or identifying reflectance color pixels for intrinsic  
 79 decomposition, *etc.* Because knapsack algorithms are aimed at finding items with as large as possible  
 80 total values and limited total weights, our verifications are presented as:

- 81 1. to verify that item value  $v_p$  is positively correlated to task-specific desired patterns.
- 82 2. to verify that item weight  $w_p$  is negatively correlated to task-specific desired patterns.

### 83 1.2 Setup

84 We use texture removal task to verify our modeling. In particular, we use RTV Texture Boundary  
 85 (RTVDB) dataset in [Xu et al. \[2012\]](#) to obtain in-the-wild image instances and the paired texture  
 86 annotations. [Xu et al. \[2012\]](#) provides 200 textured images and 200 paired human annotated structure

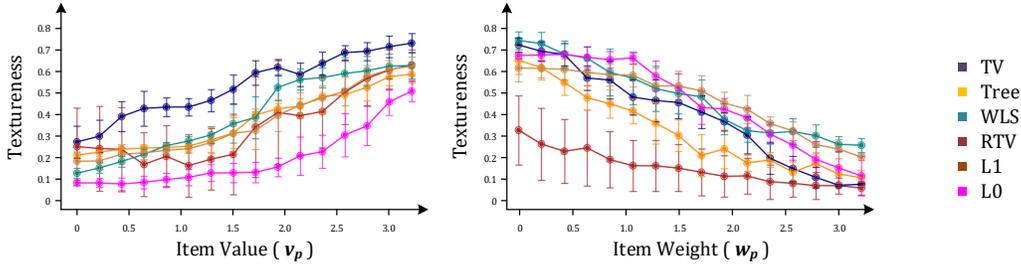


Figure 2: Correlation between our item value/weight modeling and ground truth texturalness.

87 boundary maps. We measure pixel-wise distance to nearest structure boundary as structuralness (and  
 88 the inverted value as texturalness). As shown in Fig.1, pixels with dense and continuous texture are  
 89 annotated with high texturalness (low structuralness) whereas pixels over structural edges or object  
 90 boundaries are marked with low texturalness (high structuralness).

### 91 1.3 Involved image smoothing energy

92 We exploit various image smoothing energies ( WLS, Welsch [1977]; TV, RUDIN et al. [1992];  
 93 L0, Xu et al. [2011]; RTV, Xu et al. [2012]; TREE, Bao et al. [2014]; L1, Bi et al. [2015]) in this  
 94 verification.

### 95 1.4 Implementation details

96 Using all involved methods, we perform smoothing on all image instances in the RTVDB dataset and  
 97 randomly sample one million pixel position points in all smoothed images. For each point, we obtain  
 98 the measured item value, item weight, and the ground truth texturalness.

### 99 1.5 Verification

100 As in Fig. 2, we report the obtained correlation between item weight, item value, and texturalness. We  
 101 divide all values/weights into 16 bins and then report the mean value and standard deviation in each  
 102 bin for each candidate. Regardless of various frontend smoothing energies,  $v_p$  always shows positive  
 103 correlation with ground truth texturalness. In the meanwhile,  $w_p$  always shows negative correlation  
 104 with the texturalness. These evidences verify that our modeling has solid foundations in the texture  
 105 removal tasks. Given the typicality of texture removal in image smoothing, our approach in other  
 106 related tasks is likely to have similar verifications. These evidences also shows that our knapsack  
 107 modeling is statistically well-motivated and technically solid to tackle specific problems.

## 108 2 Algorithmic Backgrounds: 0-1 Knapsack

109 The 0-1 knapsack problem is one of the most typical combinatorial problem in mathematics, statistics,  
 110 and economics. Given a set of items, each with a weight and a value, the objective is to determine  
 111 whether to include each item in a collection so that the total weight is less than or equal to a given  
 112 limit and the total value is as large as possible.

113 Dynamic Programming (DP) 0-1 knapsack solver is one of the most typical solutions for this problem.  
 114 A python version of this standard solver can be sketched as:

---

```

# Python code of standard 0-1 knapsack dynamic programming (DP) solver.

def knapsack_01(n, c, w, v):
    value = [[0 for j in range(int(c) + 1)] for i in range(n + 1)]
    for i in range(1, n + 1):
        for j in range(1, int(c) + 1):
            value[i][j] = value[i - 1][j]
            if j >= w[i - 1] and value[i][j] < value[i - 1][int(j - w[i - 1])] + v[i - 1]:
                value[i][j] = value[i - 1][int(j - w[i - 1])] + v[i - 1]
    x = [0 for i in range(n)]
    j = c
    for i in range(n, 0, -1):
        if value[i][int(j)] > value[i - 1][int(j)]:
            x[i - 1] = 1
            j -= w[i - 1]
    return x

# Below is a unit test for this function.

knapsack_capability = 5
item_quantity = 6
test_weights = [2.4, 2.6, 3.2, 1.2, 5.7, 2.9]
test_values = [2.7, 3.2, 1.6, 5.3, 4.3, 3.1]
test_result = knapsack_01(item_quantity, knapsack_capability, test_weights, test_values)
print(test_result)

```

---

117 It is worth noticing that the time complexity of this standard solver is  $O(NW)$  with  $N$  being the item  
118 quantity and  $W$  being the (integer number of) the knapsack capability. This solver may yield optimal  
119 solutions, nevertheless it may also consume hours to compute one large image with pixel quantity at  
120 about  $1e8$ . Therefore, it is important to apply some basic accelerations for practical usages.

## 121 2.1 Scalable 0-1 knapsack solver

122 The problem of scaling 0-1 Knapsack algorithm is extensively studied in the field of mathematics  
123 and statistics. We adopt a simple yet very effective solver using Stanford Greedy Knapsack Heuristic  
124 (GKH, [Stanford \[2001\]](#)).

125 The basic idea is that, instead of testing all items in or out of the knapsack, we may only compute  
126 a relatively small subset of all items so that a vast majority of the time consuming can be saved.  
127 When the knapsack capability is extremely large, the target items can be viewed as particles with the  
128 value-weight density  $d_p$

$$d_p = \frac{v_p}{w_p} \quad (3)$$

129 For each item  $p$ , if the density  $d_p$  is very large, we can assume that this item is of great value and  
130 then directly put it into the knapsack without extra consideration. On the contrary, if the density  $d_p$   
131 is minimal, we may directly ignore it because it may not make much contribution to our value-weight  
132 trade-offs. Finally, when the density  $d_p$  is neither too large nor too small, we apply standard knapsack  
133 algorithm to solve these mid-range items.

134 In particular, given the knapsack capability  $U$ , we first roughly estimate item quantity  $\bar{Q}$  in the  
135 knapsack

$$\bar{Q} = \frac{U}{\bar{d}} \quad (4)$$

136 where  $\bar{d}$  is the average density of all items. After that, we define a parameter called *interested range*  
137 denoted by  $N_{\text{interested}}$ . Given a set of item densities  $\mathbf{d}_{1\dots N}$  sorted from small to large, we divide them  
138 into three groups

$$\{\mathbf{d}_1, \dots, \mathbf{d}_N\} \rightarrow \{\mathbf{d}_1, \dots, \mathbf{d}_{\bar{Q} - \frac{1}{2}N_{\text{interested}}}\} + \{\mathbf{d}_{\bar{Q} - \frac{1}{2}N_{\text{interested}}}, \dots, \mathbf{d}_{\bar{Q} + \frac{1}{2}N_{\text{interested}}}\} + \{\mathbf{d}_{\bar{Q} + \frac{1}{2}N_{\text{interested}}}, \dots, \mathbf{d}_N\} \quad (5)$$

139 where  $N_{\text{interested}} = 200$  is a good choice for large images. All items in  $\{\mathbf{d}_1, \dots, \mathbf{d}_{\bar{Q} - \frac{1}{2}N_{\text{interested}}}\}$   
140 are directly excluded from the knapsack, and all items in  $\{\mathbf{d}_{\bar{Q} + \frac{1}{2}N_{\text{interested}}}, \dots, \mathbf{d}_N\}$  are directly  
141 included in the knapsack. After that, we solve the standard 0-1 knapsack within the subset  
142  $\{\mathbf{d}_{\bar{Q} - \frac{1}{2}N_{\text{interested}}}, \dots, \mathbf{d}_{\bar{Q} + \frac{1}{2}N_{\text{interested}}}\}$ . A python version of this accelerated solver can be sketched as:

---

```

143 # python code of Greedy Knapsack Heuristic (GKH) 01 knapsack solver.
144
145 def knapsack_01_GKH(sorted_item_indices, Q_bar, N_interested, n, c, w, v):
146     x = [0 for i in range(n)]
147     # exclude items with low density
148     x[0: Q_bar - N_interested // 2] = 0
149     # include items with high density
150     x[Q_bar + N_interested // 2: n] = 1
151     # analyse interested items with mid-range density
152     n -= N_interested
153     c = N_interested
154     v = [v[sorted_item_indices[i]] for i in range(Q_bar - N_interested // 2, Q_bar + N_interested // 2)]
155     w = [w[sorted_item_indices[i]] for i in range(Q_bar - N_interested // 2, Q_bar + N_interested // 2)]
156     x[Q_bar - N_interested // 2: Q_bar + N_interested // 2] = knapsack_01(n, c, w, v)
157     return x

```

---

145 With this improved solver,  $512 \times 512$  pixels can be solved in roughly 175 ms as reported in the main  
146 article. This implementation can significantly speed up the solving, and almost no visual quality  
147 sacrifice is caused in human perception.

## 148 2.2 Stabilized solver and full implementation codes

149 As in the main paper, the actual knapsack problem is solved in multiple iterations. This solver can  
150 be further stabilized by introducing randomness. For example, we can add some random noise in  
151 some starting iterations and then progressively remove these noise when nearing convergence. This  
152 *simulated annealing* trick can contribute to the robustness of the solver.

153 Furthermore, we provide full codes of our knapsack solver implementation in the *code-and-data* files  
154 to aid in reproducibility.

## 155 3 Image Smoothing Implementation Details

156 We clarify detailed implementation applying EAP to different image smoothing energies.

### 157 3.1 EAP + Total Variation

158 The total variation (RUDIN et al. [1992]) smoothing energy can be written in form of the formulation  
159 in the main article as

$$\rho(\mathbf{Y}) = \lambda(|\partial_x \mathbf{Y}| + |\partial_y \mathbf{Y}|) \quad (6)$$

160 where  $\mathbf{Y}$  is the image for optimization.  $\partial_x \mathbf{Y}$  or  $\partial_y \mathbf{Y}$  refers to image gradient in x-axis or y-axis.  
161 Total variation is relatively easy to implement and we use gradient descent method to solve the  
162 smoothing problem. Note that we have two options to apply EAP: (a) solve knapsack each time after  
163 total variation is converged, or (b) solve knapsack for each total variation minimization iteration.  
164 Nevertheless, we find these two methods yields nearly same visual results. We recommend to use (a)  
165 for implementation flexibility. We fix  $\lambda = 0.1$  in experiments.

### 166 3.2 EAP + Weighted Least Square

167 Weighted least square (Welsch [1977]) energy can be formulated for each pixel position  $p$  as

$$\rho(\mathbf{Y})_p = \lambda \sum_{i \in l_p} \exp(-\|Y_p - Y_i\|/\sigma_s) \|Y_p - Y_i\|_2^2 \quad (7)$$

168 which is fully differentiable and can be implemented in the same way as total variation. We fix  $l_p$  as a  
169  $3 \times 3$  window,  $\lambda = 0.1$ , and  $\sigma_s = 0.25$  in experiments.

### 170 3.3 EAP + L0 Smoothing

171 L0 smoothing (Xu et al. [2011]) energy can be formulated as

$$\rho(\mathbf{Y}) = \lambda(\#\partial_x \mathbf{Y} + \#\partial_y \mathbf{Y}) \quad (8)$$

172 where  $\#$  is the counting metric outputting the quantity of non-zero elements in a matrix. L0 smoothing  
173 has closed-form solvers. Official L0 smoothing implementation recommends to use fast Fourier

174 transform to preserve source image appearance, causing a bit troublesome to apply EAP to get rid of  
 175 appearance preservation. Our solution is to use [Xu et al. \[2011\]](#)'s secondary gradient descent solver  
 176 to replace Fourier transform so that EAP can be easily implemented. Note that this modification does  
 177 not numerically change the results because the Fourier transform solver and the gradient descent  
 178 solver yield mathematically same results as mentioned in [Xu et al. \[2011\]](#). We fix  $\lambda = 0.01$  in  
 179 experiments.

### 180 3.4 EAP + Relative Total Variation

181 Relative total variation ([Xu et al. \[2012\]](#)) energy can be formulated as:

$$\rho(\mathbf{Y})_p = \lambda \left( \frac{\mathfrak{D}_x(p)}{\mathfrak{L}_x(p) + \epsilon} + \frac{\mathfrak{D}_y(p)}{\mathfrak{L}_y(p) + \epsilon} \right) \quad (9)$$

182 where the term of  $\mathfrak{D}(\cdot)$  is defined as

$$\mathfrak{D}_x(p) = \sum_{q \in l_p} g_{pq} |\partial_x \mathbf{Y}_q| \quad \text{and} \quad \mathfrak{D}_y(p) = \sum_{q \in l_p} g_{pq} |\partial_y \mathbf{Y}_q| \quad (10)$$

183 and  $\mathfrak{L}(\cdot)$  is defined as

$$\mathfrak{L}_x(p) = \left| \sum_{q \in l_p} g_{pq} \partial_x \mathbf{Y}_q \right| \quad \text{and} \quad \mathfrak{L}_y(p) = \left| \sum_{q \in l_p} g_{pq} \partial_y \mathbf{Y}_q \right| \quad (11)$$

184 and  $g_{pq}$  is defined as

$$g_{pq} = \exp \left( - \frac{(p_x - q_x)^2 + (p_y - q_y)^2}{2\sigma^2} \right) \quad (12)$$

185 and the default parameters are  $3 \times 3$  window  $l_p$ ,  $\sigma = 0.2$ , and  $\lambda = 0.015$ . Official relative total  
 186 variation solver is numerical, and the objective is solved iteratively in a two-step manner. We replace  
 187 its original appearance approximation with EAP in the *structure extraction* step and the other step  
 188 remains same.

### 189 3.5 EAP + Spanning Tree

190 It is worth noticing that Spanning Tree ([Bao et al. \[2014\]](#)) is particularly a filtering method rather than  
 191 an optimization-based method. We include this method because it is typical and common-used, and it  
 192 also has optimization-based versions. The formulation of optimization-based spanning tree energy is

$$\rho(\mathbf{Y})_p = \lambda \left\| \mathbf{Y}_p - \sum_{j \in \tilde{h}} w_p(j) \mathbf{Y}_j \right\|_2^2 \quad (13)$$

193 where  $\tilde{h}$  is the set of all pixel positions and  $w_p(\cdot)$  is the *Spanning Tree Collaborative Weight*. The  
 194 term  $w_p(\cdot)$  inherently obeys the global addend constraints

$$\left\{ \sum_{j \in \tilde{h}} w_p(j) = 1 \mid \forall p \in \tilde{h} \right\} \quad (14)$$

195 and for more details please refer to [Bao et al. \[2014\]](#). EAP can also be implemented using this  
 196 smoothing energy with default parameter  $\lambda = 0.1$ .

### 197 3.6 EAP + L1 smoothing

198 L1 smoothing ([Bi et al. \[2015\]](#)) energy can be formulated as:

$$\rho(\mathbf{Y})_p = \lambda_1 \left( \sum_{i \in l_p} \sum_{j \in l_p} w_{ij} \|\mathbf{Y}_i - \mathbf{Y}_j\|_2 \right) + \lambda_2 \left( \sum_{i \in g_p} \sum_{j \in g_p} w_{ij} \|\mathbf{Y}_i - \mathbf{Y}_j\|_2 \right) \quad (15)$$

199 where  $w_{ij}$  is the weight for color distance in weighted CIE-Lab space.  $l_p$  is a local window at  $p$ ,  
 200 and  $g_p$  is a super-pixel region that contains  $p$ . We use the recommended official configurations  
 201  $\lambda_1 = 20.00$ ,  $\lambda_2 = 0.01$ , and all parameters are same as official implementations. So EAP can be  
 202 directly embedded to the official Split-Bregman solver.

## 203 **4 Ablative Study Implementation Details**

204 We detail the ablative study in the main paper.

### 205 **4.1 Official Implementations**

206 We present the smoothed results using official implementations of different image smoothing algo-  
207 rithms.

### 208 **4.2 Extreme Parameter**

209 We present the smoothed results using extreme lambda in different image smoothing algorithms, but  
210 without using EAP. In the main paper we have presented results using L1 smoothing ( $\lambda = 10.0$ ). In  
211 the supplementary material we present results with some other configurations: (1) L0 smoothing and  
212  $\lambda = 0.1$ . (2) RTV and  $\lambda = 0.2$ . (3) L1 smoothing and  $\lambda = 5$ . Please see also Fig. 6-10 for details.

### 213 **4.3 Iterative Smoothing**

214 We present the smoothed results by repeating original image smoothing algorithms multiple times  
215 (10 times, same as the our default EAP configuration), but without using EAP. In the main paper  
216 we have presented results using L1 smoothing (repeating 10 times). In the supplementary material  
217 we present results with some other configurations: (1) L0 smoothing (repeating 10 times). (2) RTV  
218 (repeating 10 times). (3) L1 smoothing (repeating 10 times). Please see also Fig. 6-10 for details.

### 219 **4.4 Without Weight**

220 We present the smoothed results without using knapsack weights  $w_p$ . We set a fixed threshold (0.1)  
221 to the knapsack values  $v_p$ . All pixels above this threshold are viewed as erasing positions. The results  
222 are presented in the main paper.

### 223 **4.5 Meaningless Weight**

224 We present the smoothed results by replacing all knapsack weights  $w_p$  with a constant (1.0). The  
225 results are presented in the main paper.

### 226 **4.6 Without Value**

227 We present the smoothed results without using knapsack values  $v_p$ . We set a fixed threshold (0.1) to  
228 the knapsack weights  $w_p$ . All pixels above this threshold are viewed as erasing positions. The results  
229 are presented in the main paper.

### 230 **4.7 Meaningless Value**

231 We present the smoothed results by replacing all knapsack value  $v_p$  with a constant (1.0). The results  
232 are presented in the main paper.

### 233 **4.8 Full Method**

234 Our proposed solution with 0-1 knapsack solving. The results are presented in the main paper.

## 235 **5 Image Decomposition Implementation Details**

### 236 **5.1 EAP + DPGMM + L1 smoothing**

237 [Bi et al. \[2015\]](#) proposes to smooth images in multiple stages. After a standard L1 smoothing, this  
238 technique applies Dirichlet Process Gaussian Mixture Model (DPGMM) to cluster all pixels into an

239 adaptive quantity of clusters. After that, this technique smooths images again. A rough formulation  
 240 could be written as

$$\rho(\mathbf{Y})_p = \lambda_1 \left( \sum_{i \in l_p} \sum_{j \in l_p} w_{ij} \|\mathbf{Y}_i - \mathbf{Y}_j\|_2 \right) + \lambda_2 \left( \sum_{i \in g_p} \sum_{j \in g_p} w_{ij} \|\mathbf{Y}_i - \mathbf{Y}_j\|_2 \right) + \lambda_3 \left( \sum_{i \in c_p} \sum_{j \in c_p} w_{ij} \|\mathbf{Y}_i - \mathbf{Y}_j\|_2 \right) \quad (16)$$

241 where  $c_p$  is a DPGMM cluster that contains pixel position  $p$ , and all other terms remain same with L1  
 242 smoothing. For more implementation details please refer to [Bi et al. \[2015\]](#). This method is aimed at  
 243 building up object-wise color consistency for intrinsic decomposition. This smoothing energy can be  
 244 directly implemented in the same way with L1 smoothing.

## 245 5.2 EAP + Bell

246 Bell ([Bell et al. \[2014\]](#)) method is a very typical intrinsic decomposition method. Its optimization  
 247 is discrete and it does not explicitly require appearance preserving. However, the appearance  
 248 preservation is in particular hidden in its formulations. Many other intrinsic decomposition methods  
 249 can be formulated in similar ways as Bell method. The embedding of EAP into Bell can be applied to  
 250 many other intrinsic methods.

251 Given the image  $\mathbf{X}$ , Bell method solves a reflectance map  $\mathbf{R}$  and a shading map  $\mathbf{S}$  so that

$$\mathbf{X} = \mathbf{R} \odot \mathbf{S} \quad (17)$$

252 where  $\odot$  is the Hadamard product. Bell’s overall optimization can be written as

$$E_{\text{intrinsic}} = E_{\text{reflectance}}(\mathbf{R}) + E_{\text{shading}}(\mathbf{S}) \quad \text{s.t.} \quad \mathbf{X} = \mathbf{R} \odot \mathbf{S} \quad (18)$$

253 In Bell method, the term  $E_{\text{reflectance}}$  includes *pairwise reflectance prior*, *shading smoothness prior*,  
 254 *absolute shading intensity prior*, and  $E_{\text{shading}}$  includes *shading discontinuity prior*. For detailed  
 255 formulations, please refer to [Bell et al. \[2014\]](#). Among all involved prior constraints, no explicit  
 256 appearance preservation can be found. However, Bell’s appearance preservation is in particular  
 257 hidden in their priors.

258 Taking their *shading discontinuity prior* as an example, which can be written as

$$e_{\text{discontinuity}} = \sum_{(i,j) \in B} |\log \mathbf{S}_i - \log \mathbf{S}_j| \quad (19)$$

259 where  $B$  is a set of many pixel position pairs  $(i, j)$ , and in each pair,  $i$  and  $j$  are two adjacent pixel  
 260 positions. We can transform this constraint into

$$\begin{aligned} e_{\text{discontinuity}} &= \sum_{(i,j) \in B} \left| \log \frac{\mathbf{X}_i}{\mathbf{R}_i} - \log \frac{\mathbf{X}_j}{\mathbf{R}_j} \right| \\ &= \sum_{(i,j) \in B} |\log \mathbf{X}_i - \log \mathbf{R}_i - \log \mathbf{X}_j + \log \mathbf{R}_j| \\ &= \sum_{(i,j) \in B} |(\log \mathbf{X}_i - \log \mathbf{X}_j) - (\log \mathbf{R}_i - \log \mathbf{R}_j)| \\ &= \sum_{(i,j) \in B} |\partial_i \log \mathbf{X}_i - \partial_i \log \mathbf{R}_i| \end{aligned} \quad (20)$$

261 According to Poisson [Perez et al. \[2003\]](#) opinion, when the sampled points in  $B$  are dense enough,  
 262 the approximation of image gradients can be viewed as that for the definite integral of image intensity

$$\begin{aligned} \int_0^i e_{\text{discontinuity}} &= \int_0^i \sum_{(i,j) \in B} |\partial_i \log \mathbf{X}_i - \partial_i \log \mathbf{R}_i| \\ &= \sum_{(i,j) \in B} \int_0^i |\partial_i \log \mathbf{X}_i - \partial_i \log \mathbf{R}_i| \\ &\approx \sum_{(i,j) \in B} |\log \mathbf{X}_i - \log \mathbf{R}_i| \end{aligned} \quad (21)$$

263 That is to say, Bell’s *shading discontinuity prior* is in particular mathematically consistent to the  
 264 log-space appearance preservation between source image  $\mathbf{X}$  and smoothed reflectance  $\mathbf{R}$ .

265 Similarly, Bell’s *shading smoothness prior* can be written as

$$\begin{aligned}
 e_{\text{shading\_smoothness}} &= \sum_i (\log \mathbf{S}_i - \log \mathbf{S}_{i+1})^2 \\
 &= \sum_i \left( \log \frac{\mathbf{X}_i}{\mathbf{R}_i} - \log \frac{\mathbf{X}_{i+1}}{\mathbf{R}_{i+1}} \right)^2 \\
 &= \sum_i \left( (\log \mathbf{X}_i - \log \mathbf{X}_{i+1}) - (\log \mathbf{R}_i - \log \mathbf{R}_{i+1}) \right)^2 \\
 &= \sum_i (\partial_i \log \mathbf{X}_i - \partial_i \log \mathbf{R}_i)^2 \\
 \int_0^i e_{\text{shading\_smoothness}} &\approx \sum_i (\log \mathbf{X}_i - \log \mathbf{R}_i)^2
 \end{aligned} \tag{22}$$

266 where the *shading discontinuity prior* can also be written as log-space appearance preservation.

267 Finally, Bell’s *absolute shading intensity prior* can also be transformed

$$\begin{aligned}
 e_{\text{absolute\_shading\_intensity}} &= \sum_i |\log \mathbf{S}_i - \log \bar{\mathbf{S}}| \\
 &= \sum_i |\log \mathbf{X}_i - \log \mathbf{R}_i - \log \bar{\mathbf{S}}| \\
 &= \sum_i |\log \mathbf{X}_i - \log \mathbf{R}_i \cdot \bar{\mathbf{S}}|
 \end{aligned} \tag{23}$$

268 where  $\bar{\mathbf{S}}$  is the average value of  $\mathbf{S}$ . That is to say, the *absolute shading intensity prior* is transformed  
 269 into log-space appearance preservation between the scaled source  $\mathbf{X}$  and smoothed reflectance  $\mathbf{R}$ .

270 In particular, we apply EAP to all these appearance preservation terms. We compute the 0-1 knapsack  
 271 using source image  $\mathbf{X}$  and smoothed reflectance image  $\mathbf{R}$ , and then replace the three mentioned  
 272 priors with their EAP versions.

273 Many other intrinsic methods can be implemented in the same way by finding the hidden appearance  
 274 preservation in their priors and then apply EAP to getting rid of their appearance preservation terms.

275 Besides, the original Bell method recommends to only compute reflectance intensity whereas ignore  
 276 the reflectance hue/saturation (or called chroma). We obey this principle in all quantitative compar-  
 277 isons to ensure the fairness and that its performance is consistent to previous literature. However, we  
 278 also find that its image editing usability and capability can be improved if it computes all reflectance  
 279 channels. Therefore, in our human-involved interactive user study, we use the Bell to compute all  
 280 reflectance channels to make the evaluation more perception-based.

### 281 5.3 EAP + Advanced image decomposition

282 [Carroll et al. \[2011\]](#) proposes to decompose illumination maps given reflectance maps and appearance  
 283 maps. In main paper we directly view this method as a black-box and it is not necessary to make  
 284 more modifications.

285 One important notice is that this technique is in particular an interactive application. Users can  
 286 use scribbles to control the decomposed layers. However, all results in the our work are obtained  
 287 automatically without any extra interaction.

## 288 6 Image Manipulation Implementation Details

289 Given a set of image editing layers, *i.e.*, Adobe PhotoShop Layers, we here clarify some terminologies  
 290 mentioned in the main article. We illustrate some examples in Fig. 3 and Fig. 4.

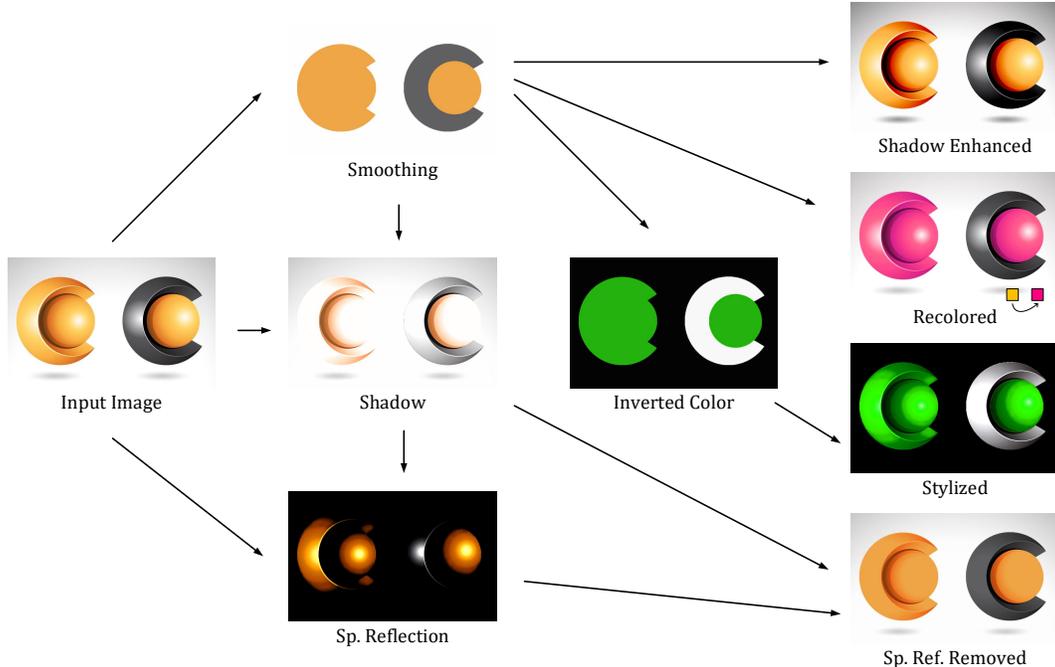


Figure 3: Toy examples of involved image editing workflows in our experiments.

291 **6.1 Layer removal or reordering**

292 Users may directly remove any layer or change the order of some layers. These are fundamental use  
 293 cases of layer-based image editing.

294 **6.2 Color inverting**

295 Users may also invert the layer colors. This is useful when the objective is to recoloring reflectance  
 296 layers or invert illumination conditions, *i.e.* black-to-white object recoloring, day-to-night relighting,  
 297 *etc.*

298 **6.3 Curves tuning and Exposure/Gamma correction**

299 Users may tune the intensity curves of any specific layers. In particular, exposure tuning and gamma  
 300 correction are frequently used cases. Given user-specified exposure scaler  $k$  and gamma scaler  $g$ , the  
 301 mapping can be sketched as

$$y = (kx)^g \quad (24)$$

302 where  $y$  is output intensity and  $x$  is input intensity. Note that this transform can be applied to any  
 303 single layer, multiple selected layers, or all layers.

304 **6.4 Masking**

305 Because EAP smoothing method yields highly structured color maps, we can use very simple  
 306 transforms to obtain high-quality masks. In particular, given a smoothed structure  $\mathbf{Y}$  and a user-given  
 307 source color  $\mathbf{c}_s \in \mathbb{R}^3$ , a mask  $\mathbf{M}$  can be measured as

$$\mathbf{M}_p = \lambda \|\mathbf{Y}_p - \mathbf{c}_s\|_2^2 \quad (25)$$

308 where  $\lambda$  is a scaler to normalize this mask. Note that this mask is not binarized, and it is a soft  
 309 segmentation of the source image. This mask can be applied to many use cases to separately editing  
 310 image constitutes. Because  $\mathbf{c}_s$  can be sampled with only one click in images, it is very flexible to  
 311 obtain the mask  $\mathbf{M}$ .

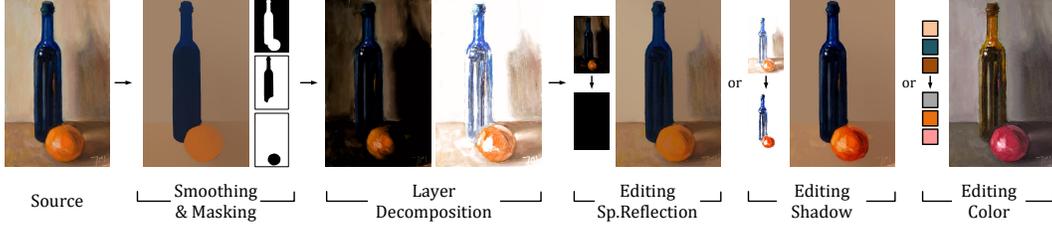


Figure 4: Typical image manipulation using strategies involved in our image editing experiments.

## 312 6.5 Recoloring

313 Given source color  $c_s \in \mathbb{R}^3$  and target color  $c_t \in \mathbb{R}^3$ , a directional color vector  $c_v$  can be written as

$$c_v = c_t - c_s \quad (26)$$

314 Then, using the mask  $M$ , users may directly manipulate the appearance colors in image  $X$

$$X_p^* = M_p \odot c_v + X_p \quad (27)$$

315 where  $\odot$  is the Hadamard product, and  $X^*$  is the edited image. Note that this formulation is only a  
 316 basic and simple recoloring maneuver and advanced image recoloring is extensively studied in methods  
 317 like [Carroll et al. \[2011\]](#); [Tan et al. \[2016, 2018\]](#). Finally, this recoloring can be applied to any single  
 318 or multiple decomposed layers.

## 319 7 IIW/SAW Test Implementation Details

320 One notice is that some intrinsic methods output single-channel gray-scale illumination maps whereas  
 321 some others yield colorful illumination maps. Because IIW/SAW is focused on single-channel  
 322 illumination, we convert all available illumination maps into gray-scale in IIW/SAW tests.

### 323 7.1 Intrinsic Image in the Wild

324 As to IIW [Bell et al. \[2014\]](#) test, we directly use the official implementation to evaluate the candidates.  
 325 One notice is that L1 smoothing is very time consuming and we use the evaluation method mentioned  
 326 in [Bi et al. \[2015\]](#) to speed up the experiments.

### 327 7.2 Shadow Annotation in the Wild

328 As to SAW [Kovacs et al. \[2017\]](#) test, instead of the original metric, we use the challenged metric in [Li](#)  
 329 [and Snavely \[2018\]](#) as our measurements. The enhanced metric is considered to be able to highlight  
 330 performance differences. Similarly, for L1 smoothing we use method in [Bi et al. \[2015\]](#) to obtain the  
 331 test data.

## 332 8 Deep Learning Method Implementation Details

### 333 8.1 CGIntrinsics

334 [Li and Snavely \[2018\]](#)'s method has official open sourced implementations. We directly use their  
 335 codes and their default configurations in our experiments.

### 336 8.2 GloSH

337 [Li and Snavely \[2018\]](#) reported their method as the current quantitative state of the art in IIW/SAW  
 338 benchmarks. This method does not have open sourced implementations. The official paper [Li and](#)  
 339 [Snavely \[2018\]](#) includes all necessary details and we reproduce their results using their recommended  
 340 configurations. Our presented results on their method should only be considered as third-party  
 341 reproductions. Nevertheless, all quantitative statistics of this method are directly transferred from  
 342 their official paper.

## 343 9 User Study Implementation Details

344 Given the reflectance map  $Y$ , the illumination map  $S$ , and the source image  $X$ , we formulate several  
345 simple and fundamental illumination manipulation use cases for the user study.

346 First of all, because some intrinsic decomposition methods do not require the perfect reconstruction  
347 of the original images, which is not acceptable in image editing, instead of directly using their  
348 illumination maps  $S$ , we compute another reconstruction-guaranteed illumination map  $S^*$  as

$$S_p^* = \frac{X_p}{Y_p + \epsilon} \quad (28)$$

349 where  $\epsilon = 1e - 10$ . In this way, the decomposition is enforced to perfectly reconstruct the source  
350 image.

### 351 9.1 Shadow enhancement

352 Given a simple fixed shadow threshold  $t_s$ , we view under-threshold pixels in illumination map  $S$  as  
353 shadow, and the shadow enhancement can be formulated as

$$X_p^* = \begin{cases} Y_p (S_p^*)^2 & S_p^* < t_s \\ Y_p S_p^* & \text{Others} \end{cases} \quad (29)$$

354 where  $X_p^*$  is the manipulated image. This transform only includes a very simple gamma correction,  
355 and the results can faithfully reflect the visual quality of the decomposed layers.

### 356 9.2 Specular reflection removal

357 Given a simple fixed specular reflection threshold  $t_r$ , we view over-threshold pixels in illumination  
358 map  $S$  as specular reflections, and the specular reflection removal can be formulated as

$$X_p^* = \begin{cases} Y_p & S_p^* > t_s \\ Y_p S_p^* & \text{Others} \end{cases} \quad (30)$$

359 This transform is achieved via removing the specular reflection parts in the illumination map. It is  
360 very simple, and thus, faithful to the quality of the original decomposed layers.

### 361 9.3 Experiment setup and results

362 As mentioned in the main paper, we apply learning-based methods [Zhou et al. \[2019\]](#); [Li and Snavely](#)  
363 [\[2018\]](#), optimization methods [Bell et al. \[2014\]](#); [Bi et al. \[2015\]](#), and their EAP versions to decompose  
364 100 scenes into layers. For fairness, we do not provide independent thresholds  $t_s$  and  $t_r$  for different  
365 methods or images. We use consistent parameter  $t_s = 0.50$  and  $t_r = 0.75$  for all involved methods  
366 and images for the sake of fairness. We obtain 600 results with enhanced shadows and 600 results  
367 with specular reflections eliminated. We employ Amazon Mechanical Turk (AMT) to rank the visual  
368 quality of these results and report the obtained ranking in Table. 1 and Table. 2.

### 369 9.4 Raw user study data

370 The 1200 raw user study results are listed in the *code-and-data* files. We also present some high-  
371 resolution ones from Fig. 42 to Fig. 55.

## 372 10 Additional Results

### 373 10.1 Image smoothing results

374 We provide additional results on image smoothing from Fig. 5 to Fig. 29.

### 375 10.2 Image decomposition results

376 We provide additional results on image decomposition from Fig. 32 to Fig. 36.

377 **10.3 Intrinsic decomposition results**

378 We provide additional results on intrinsic decomposition from Fig. 38 to Fig. 41.

379 **10.4 Image manipulation results**

380 We provide additional results on image manipulation from Fig. 42 to Fig. 55.

381 **10.5 Supporting position visualizations**

382 We extend the supporting position visualization in the main article from Fig. 57 to Fig. 62.

383 **10.6 Limitation**

384 We present limitation in Fig. 63.

385 **References**

- 386 Linchao Bao, Yibing Song, Qingxiong Yang, Hao Yuan, and Gang Wang. 2014. Tree filtering Efficient structurepreserving smoothing with a  
387 minimum spanning tree. *IEEE Transactions on Image Processing* (2014). 5, 8
- 388 Sean Bell, Kavita Bala, and Noah Snavely. 2014. Intrinsic Images in the Wild. *ACM Transactions on Graphics* 33, 4 (2014). 10, 13, 14
- 389 Sai Bi, Xiaoguang Han, and Yizhou Yu. 2015. An L1 image transform for edgepreserving smoothing and scenelevel intrinsic decomposition.  
390 *ACM Transactions on Graphics* (2015). 5, 8, 9, 10, 13, 14
- 391 Robert Carroll, Ravi Ramamoorthi, and Maneesh Agrawala. 2011. Illumination decomposition for material recoloring with consistent inter-  
392 reflections. *ACM Transactions on Graphics* (2011). 11, 13
- 393 Balazs Kovacs, Sean Bell, Noah Snavely, and Kavita Bala. 2017. Shading Annotations in the Wild. *CVPR* (2017). 13
- 394 Zhengqi Li and Noah Snavely. 2018. CGIntrinsics: Better Intrinsic Image Decomposition through Physically-Based Rendering. *ECCV* (2018).  
395 13, 14
- 396 Patrick Perez, Michel Gangnet, and Andrew Blake. 2003. Poisson image editing. *ACM Transactions on Graphics* (2003). 10
- 397 RUDIN, L, OSHER, S, , FATEMI, and E. 1992. Nonlinear total variation based noise removal algorithms. *Physica D: Nonlinear Phenomena*  
398 (1992). 5, 7
- 399 Stanford. 2001. A Greedy Knapsack Heuristic. *Shortest Paths Revisited, NP-Complete Problems and What To Do About Them* (2001). 6
- 400 Jianchao Tan, Jose Echevarria, and Yotam Ginglod. 2018. Efficient palette-based decomposition and recoloring of images via RGBXY-space  
401 geometry. *ACM Transactions on Graphics* (2018). 13
- 402 Jianchao Tan, Jyh-Ming Lien, and Yotam Gingold. 2016. Decomposing Images into Layers via RGB-space Geometry. *ACM Transactions on*  
403 *Graphics* (2016). 13
- 404 Paul W Holland Roy E Welsch. 1977. Robust regression using iteratively reweighted leastsquares. *Communications in Statisticstheory and*  
405 *Methods* (1977). 5, 7
- 406 Li Xu, Cewu Lu, Yi Xu, and Jiaya Jia. 2011. Image smoothing via L0 gradient minimization. *ACM Transactions on Graphics* (2011). 5, 7, 8
- 407 Li Xu, Qiong Yan, Yang Xia, and Jiaya Jia. 2012. Structure extraction from texture via relative total variation. *ACM Transactions on Graphics*  
408 (2012). 4, 5, 8
- 409 Hao Zhou, Xiang Yu, and David W Jacobs. 2019. GLoSH: Global-Local Spherical Harmonics for Intrinsic Image Decomposition. *ICCV*  
410 (2019). 14

Table 1: Amazon Mechanical Turk (AMT) human ranking on Shadow Enhancement (SE).

Instance	CGIntrinsics	GLoSH	Bell	EAP + Bell	DL1	EAP + DL1	Instance	CGIntrinsics	GLoSH	Bell	EAP + Bell	DL1	EAP + DL1
./sample/0.webp	5	6	3	2	4	1	./sample/51.webp	6	5	3	1	4	2
./sample/1.webp	6	5	3	2	4	1	./sample/52.webp	6	5	4	1	3	2
./sample/2.webp	5	6	4	2	3	1	./sample/53.webp	6	5	3	1	4	2
./sample/3.webp	5	6	4	1	3	2	./sample/54.webp	5	6	4	2	3	1
./sample/4.webp	6	5	4	2	3	1	./sample/55.webp	5	6	4	2	3	1
./sample/5.webp	5	6	3	1	4	2	./sample/56.webp	6	5	3	2	4	1
./sample/6.webp	6	5	3	2	4	1	./sample/57.webp	6	5	3	1	4	2
./sample/7.webp	6	5	4	2	3	1	./sample/58.webp	6	5	3	2	4	1
./sample/8.webp	5	6	4	2	3	1	./sample/59.webp	6	5	3	2	4	1
./sample/9.webp	6	5	4	2	3	1	./sample/60.webp	6	5	4	2	3	1
./sample/10.webp	5	6	4	1	3	2	./sample/61.webp	6	5	4	2	3	1
./sample/11.webp	6	5	4	2	3	1	./sample/62.webp	6	5	3	2	4	1
./sample/12.webp	6	5	4	2	3	1	./sample/63.webp	5	6	4	2	3	1
./sample/13.webp	5	6	3	2	4	1	./sample/64.webp	6	5	4	2	3	1
./sample/14.webp	6	5	3	2	4	1	./sample/65.webp	5	6	4	2	3	1
./sample/15.webp	6	5	3	2	4	1	./sample/66.webp	6	2	5	3	4	1
./sample/16.webp	6	5	4	2	3	1	./sample/67.webp	6	5	3	1	4	2
./sample/17.webp	6	5	4	2	3	1	./sample/68.webp	5	6	3	2	4	1
./sample/18.webp	6	5	4	2	3	1	./sample/69.webp	5	6	4	2	3	1
./sample/19.webp	6	5	3	2	4	1	./sample/70.webp	6	5	3	1	4	2
./sample/20.webp	6	5	3	1	4	2	./sample/71.webp	6	5	3	2	4	1
./sample/21.webp	3	5	6	2	4	1	./sample/72.webp	6	2	5	3	4	1
./sample/22.webp	6	5	4	1	3	2	./sample/73.webp	5	6	3	2	4	1
./sample/23.webp	6	5	4	2	3	1	./sample/74.webp	6	1	3	5	4	2
./sample/24.webp	5	6	3	2	4	1	./sample/75.webp	6	5	3	2	4	1
./sample/25.webp	6	5	4	2	3	1	./sample/76.webp	5	6	4	2	3	1
./sample/26.webp	5	6	4	2	3	1	./sample/77.webp	6	5	3	1	4	2
./sample/27.webp	6	5	3	2	4	1	./sample/78.webp	5	6	4	2	3	1
./sample/28.webp	5	6	4	1	3	2	./sample/79.webp	6	5	3	2	4	1
./sample/29.webp	6	5	3	2	4	1	./sample/80.webp	6	5	3	1	4	2
./sample/30.webp	6	5	4	2	3	1	./sample/81.webp	6	5	4	1	3	2
./sample/31.webp	3	6	5	4	1	2	./sample/82.webp	5	6	4	2	3	1
./sample/32.webp	6	5	4	1	3	2	./sample/83.webp	5	6	4	2	3	1
./sample/33.webp	6	5	4	1	3	2	./sample/84.webp	6	5	4	2	3	1
./sample/34.webp	6	5	4	1	3	2	./sample/85.webp	6	5	4	2	3	1
./sample/35.webp	5	6	3	1	4	2	./sample/86.webp	6	5	4	2	3	1
./sample/36.webp	6	5	4	2	3	1	./sample/87.webp	6	5	4	1	3	2
./sample/37.webp	3	5	2	6	4	1	./sample/88.webp	6	5	4	2	3	1
./sample/38.webp	6	5	4	2	3	1	./sample/89.webp	6	5	4	2	3	1
./sample/39.webp	3	6	1	5	4	2	./sample/90.webp	6	5	4	2	3	1
./sample/40.webp	6	5	3	2	4	1	./sample/91.webp	3	6	2	5	4	1
./sample/41.webp	6	5	3	2	4	1	./sample/92.webp	6	5	4	2	3	1
./sample/42.webp	6	5	3	1	4	2	./sample/93.webp	6	5	3	1	4	2
./sample/43.webp	5	6	3	2	4	1	./sample/94.webp	6	5	4	2	3	1
./sample/44.webp	5	6	4	2	3	1	./sample/95.webp	5	6	4	1	3	2
./sample/45.webp	6	5	3	2	4	1	./sample/96.webp	6	5	4	2	3	1
./sample/46.webp	5	6	4	2	3	1	./sample/97.webp	6	5	4	1	3	2
./sample/47.webp	5	6	4	2	3	1	./sample/98.webp	6	5	3	1	4	2
./sample/48.webp	6	5	4	2	3	1	./sample/99.webp	6	2	5	3	4	1
./sample/49.webp	6	5	3	2	4	1	Mean	5.70	5.30	3.55	1.71	3.45	1.29
./sample/50.webp	6	5	3	1	4	2	Std	0.46	0.46	0.50	0.45	0.50	0.45

Table 2: Amazon Mechanical Turk (AMT) human ranking on Specular Reflection Removal (SRR).

Instance	CGIntrinsics	GLoSH	Bell	EAP + Bell	DL1	EAP + DL1	Instance	CGIntrinsics	GLoSH	Bell	EAP + Bell	DL1	EAP + DL1
./sample/0.webp	5	6	3	2	4	1	./sample/51.webp	5	6	3	1	4	2
./sample/1.webp	5	3	2	6	4	1	./sample/52.webp	5	6	4	2	3	1
./sample/2.webp	5	6	4	2	3	1	./sample/53.webp	5	6	3	1	4	2
./sample/3.webp	6	5	3	2	4	1	./sample/54.webp	5	6	4	2	3	1
./sample/4.webp	6	5	4	2	3	1	./sample/55.webp	5	6	3	2	4	1
./sample/5.webp	5	6	3	2	4	1	./sample/56.webp	5	6	3	1	4	2
./sample/6.webp	6	5	4	3	2	1	./sample/57.webp	5	6	3	2	4	1
./sample/7.webp	6	5	4	1	3	2	./sample/58.webp	5	3	6	2	4	1
./sample/8.webp	5	6	4	2	3	1	./sample/59.webp	5	6	3	2	4	1
./sample/9.webp	5	6	3	2	4	1	./sample/60.webp	3	6	2	5	4	1
./sample/10.webp	5	6	4	1	3	2	./sample/61.webp	5	6	4	1	3	2
./sample/11.webp	5	6	4	2	3	1	./sample/62.webp	5	6	4	2	3	1
./sample/12.webp	6	5	3	2	4	1	./sample/63.webp	5	6	4	2	3	1
./sample/13.webp	6	5	4	1	3	2	./sample/64.webp	5	6	3	1	4	2
./sample/14.webp	5	6	3	2	4	1	./sample/65.webp	5	6	3	2	4	1
./sample/15.webp	5	6	4	2	3	1	./sample/66.webp	5	6	4	2	3	1
./sample/16.webp	6	5	3	1	4	2	./sample/67.webp	5	6	4	2	3	1
./sample/17.webp	5	6	4	2	3	1	./sample/68.webp	5	6	3	2	4	1
./sample/18.webp	5	6	4	2	3	1	./sample/69.webp	5	6	3	2	4	1
./sample/19.webp	6	2	4	5	3	1	./sample/70.webp	5	6	3	1	4	2
./sample/20.webp	1	6	5	4	3	2	./sample/71.webp	4	5	6	2	3	1
./sample/21.webp	6	5	4	1	3	2	./sample/72.webp	5	6	4	2	3	1
./sample/22.webp	6	5	3	2	4	1	./sample/73.webp	6	5	3	2	4	1
./sample/23.webp	5	6	4	1	3	2	./sample/74.webp	6	5	4	1	3	2
./sample/24.webp	2	4	6	5	3	1	./sample/75.webp	5	6	4	1	3	2
./sample/25.webp	5	6	3	2	4	1	./sample/76.webp	5	6	3	2	4	1
./sample/26.webp	2	5	4	3	6	1	./sample/77.webp	5	4	3	6	1	2
./sample/27.webp	5	6	3	1	4	2	./sample/78.webp	2	6	5	4	3	1
./sample/28.webp	6	4	1	5	3	2	./sample/79.webp	6	5	3	2	4	1
./sample/29.webp	5	6	4	2	3	1	./sample/80.webp	6	5	3	2	4	1
./sample/30.webp	6	5	3	1	4	2	./sample/81.webp	5	6	3	2	4	1
./sample/31.webp	6	5	3	2	4	1	./sample/82.webp	5	6	4	2	3	1
./sample/32.webp	5	6	3	2	4	1	./sample/83.webp	6	5	3	2	4	1
./sample/33.webp	5	6	4	2	3	1	./sample/84.webp	5	6	4	1	3	2
./sample/34.webp	5	6	3	2	4	1	./sample/85.webp	5	6	4	2	3	1
./sample/35.webp	5	6	3	1	4	2	./sample/86.webp	5	6	4	1	3	2
./sample/36.webp	5	6	3	2	4	1	./sample/87.webp	1	5	3	6	4	2
./sample/37.webp	5	6	3	2	4	1	./sample/88.webp	5	6	4	1	3	2
./sample/38.webp	1	4	6	5	3	2	./sample/89.webp	6	5	3	1	4	2
./sample/39.webp	5	6	4	2	3	1	./sample/90.webp	5	6	3	1	4	2
./sample/40.webp	6	5	4	2	3	1	./sample/91.webp	6	5	4	1	3	2
./sample/41.webp	5	6	3	2	4	1	./sample/92.webp	5	6	4	2	3	1
./sample/42.webp	5	6	4	1	3	2	./sample/93.webp	5	6	4	2	3	1
./sample/43.webp	5	6	3	2	4	1	./sample/94.webp	5	6	3	2	4	1
./sample/44.webp	5	6	4	2	3	1	./sample/95.webp	5	6	4	1	3	2
./sample/45.webp	5	6	3	2	4	1	./sample/96.webp	5	6	4	1	3	2
./sample/46.webp	6	4	5	2	3	1	./sample/97.webp	5	6	4	1	3	2
./sample/47.webp	5	6	3	1	4	2	./sample/98.webp	6	5	4	2	3	1
./sample/48.webp	5	6	4	2	3	1	./sample/99.webp	5	6	4	2	3	1
./sample/49.webp	6	5	4	2	3	1	Mean	5.22	5.77	3.54	1.66	3.47	1.34
./sample/50.webp	5	6	3	1	4	2	Std	0.41	0.44	0.52	0.47	0.50	0.47



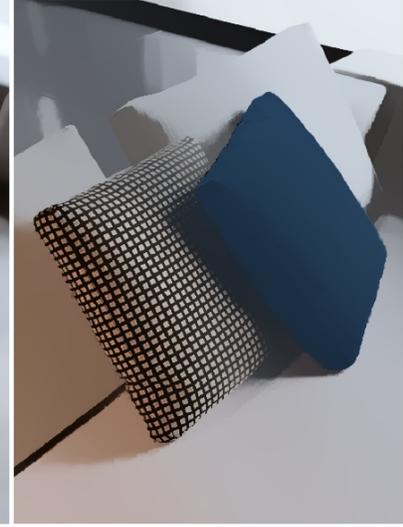
Source



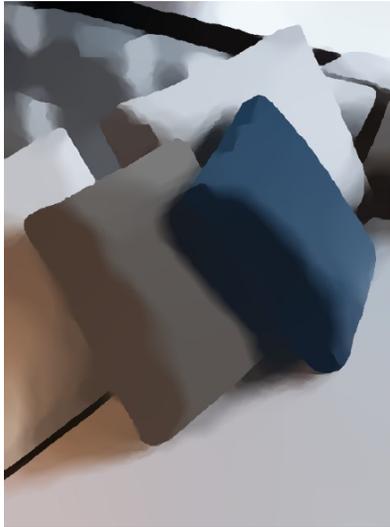
L0



RTV



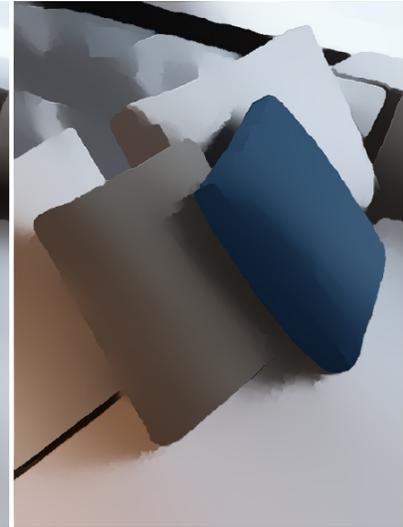
L1



EAP + L0



EAP + RTV

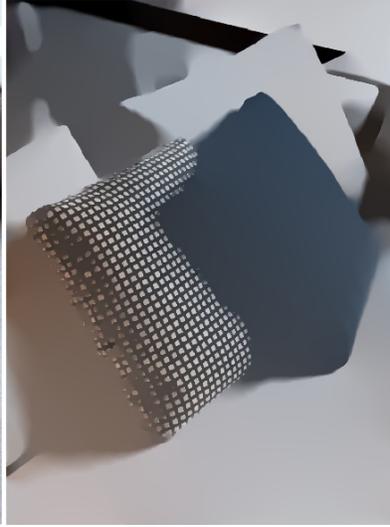


EAP + L1

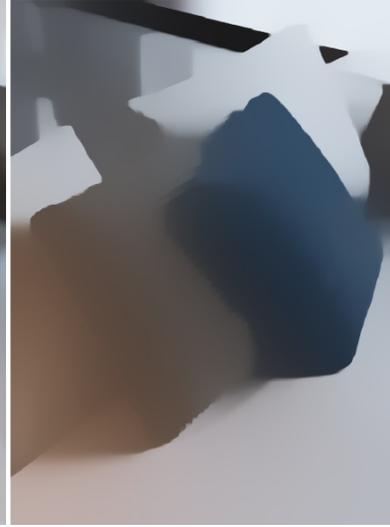
Figure 5: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.



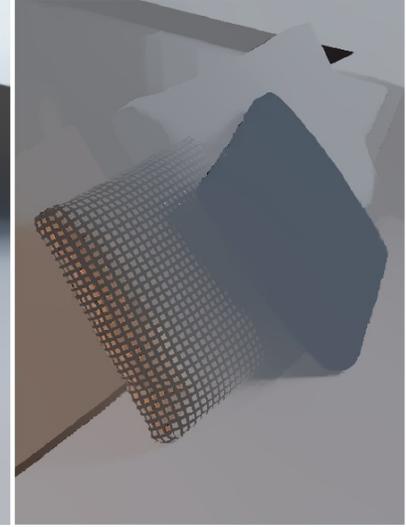
Source



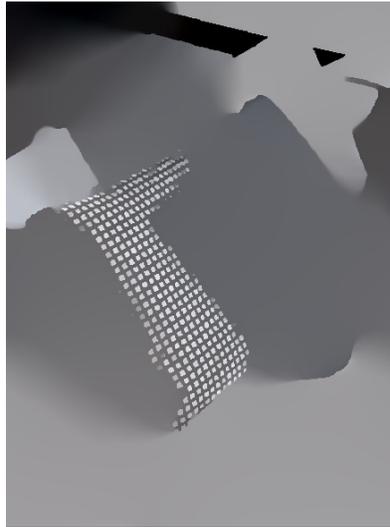
L0 (extreme parameter  $\lambda=0.1$ )



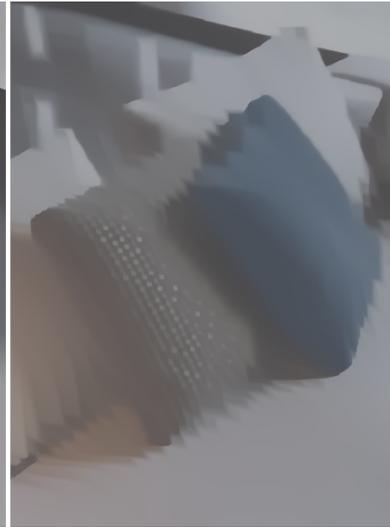
RTV (extreme parameter  $\lambda=0.2$ )



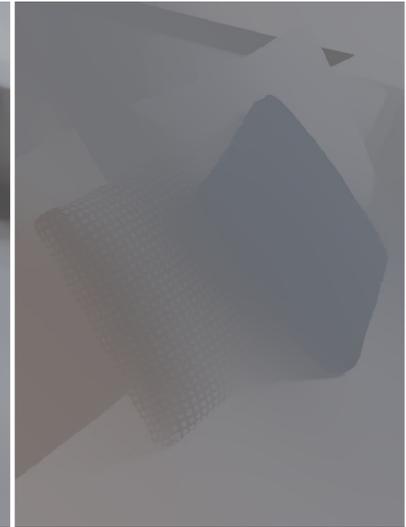
L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)  
(default official parameters)

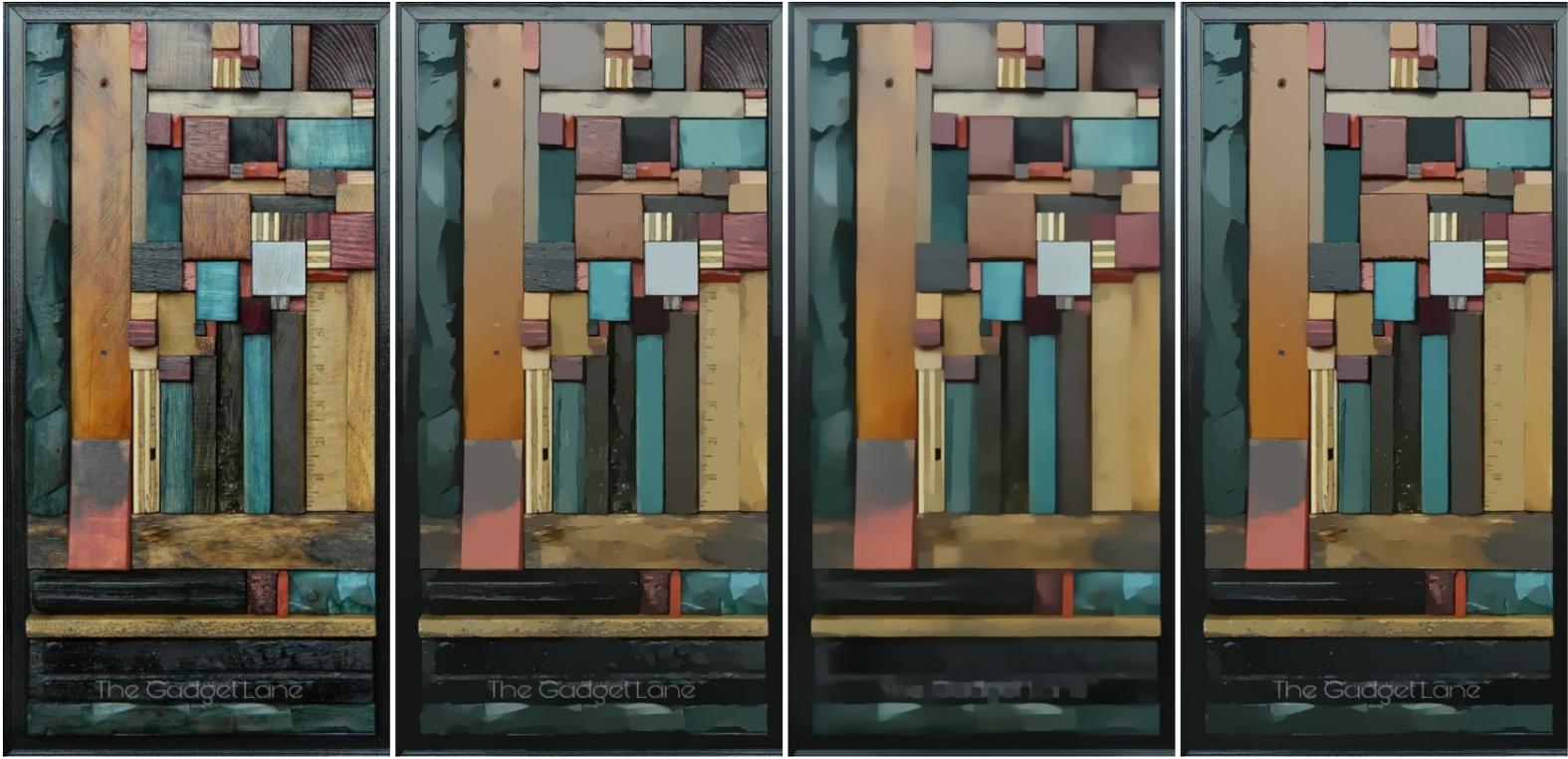


RTV (repeat 10 times)  
(default official parameters)



L1 (repeat 10 times)  
(default official parameters)

Figure 6: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.

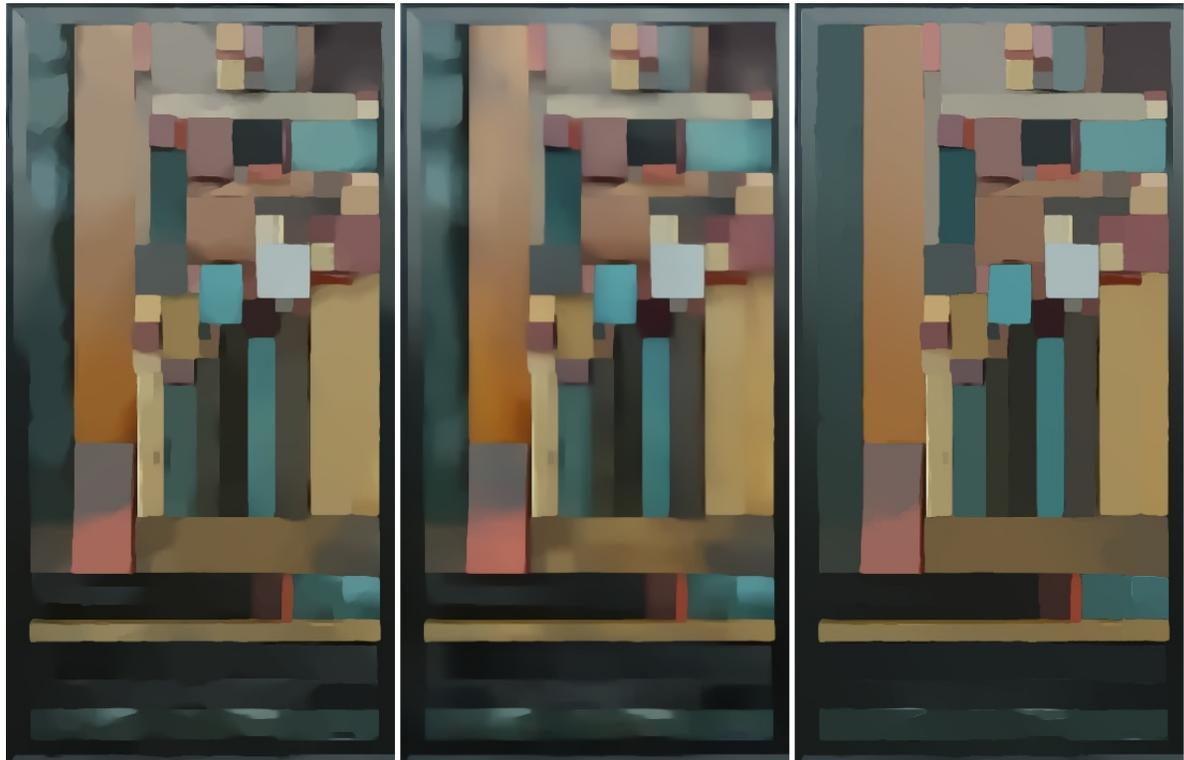


Source

L0

RTV

L1



EAP + L0

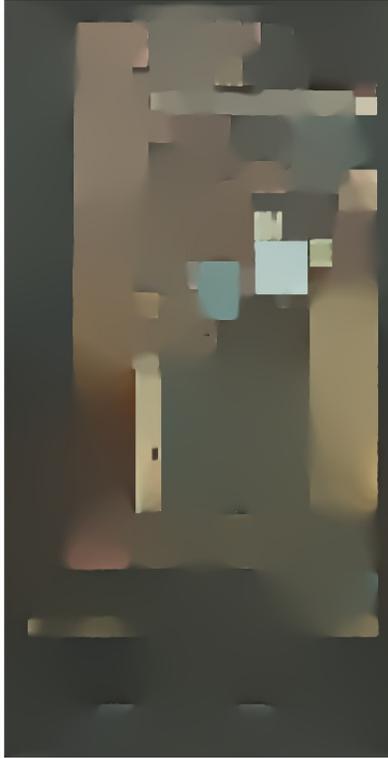
EAP + RTV

EAP + L1

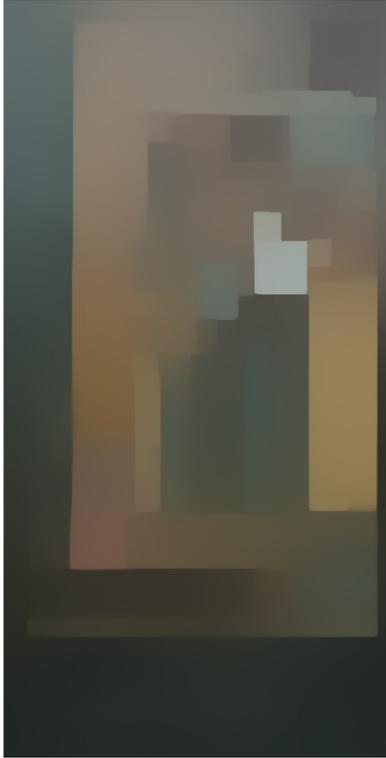
Figure 7: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.



Source



L0 (extreme parameter  $\lambda=0.1$ )



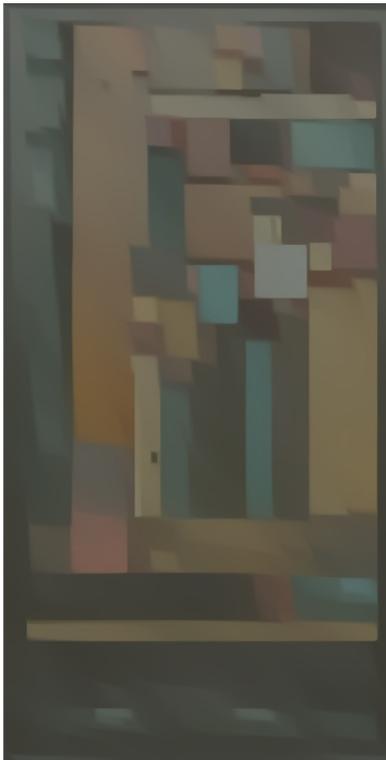
RTV (extreme parameter  $\lambda=0.2$ )



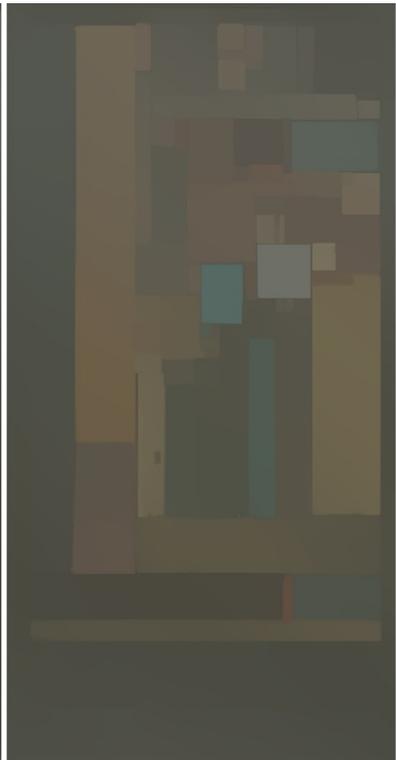
L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)  
(default official parameters)



RTV (repeat 10 times)  
(default official parameters)



L1 (repeat 10 times)  
(default official parameters)

Figure 8: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.



Source



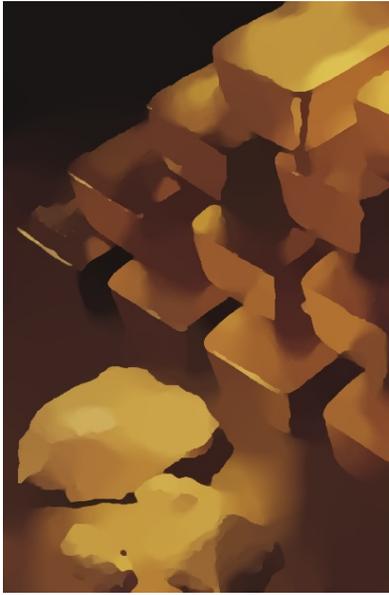
L0



RTV



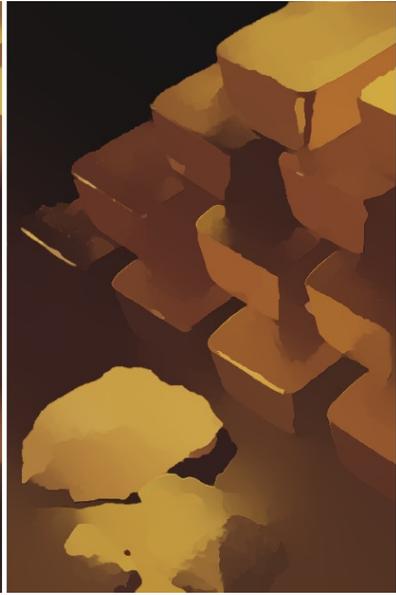
L1



EAP + L0

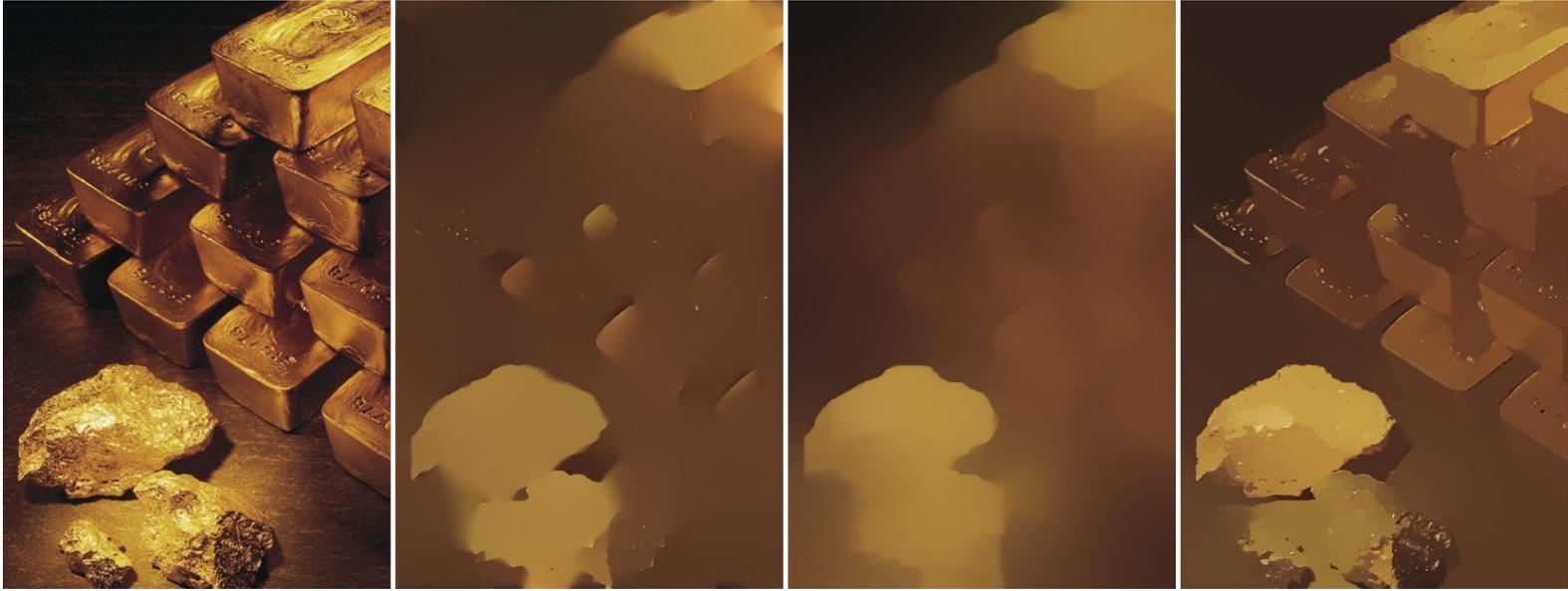


EAP + RTV



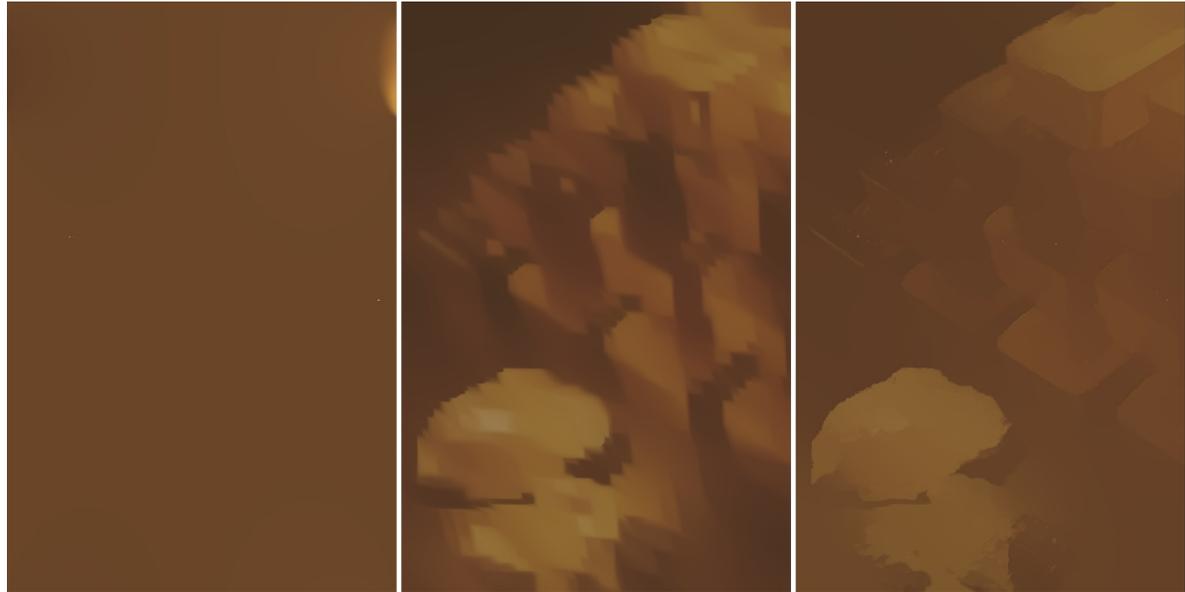
EAP + L1

Figure 9: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.



Source

L0 (extreme parameter  $\lambda=0.1$ ) RTV (extreme parameter  $\lambda=0.2$ ) L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)

RTV (repeat 10 times)

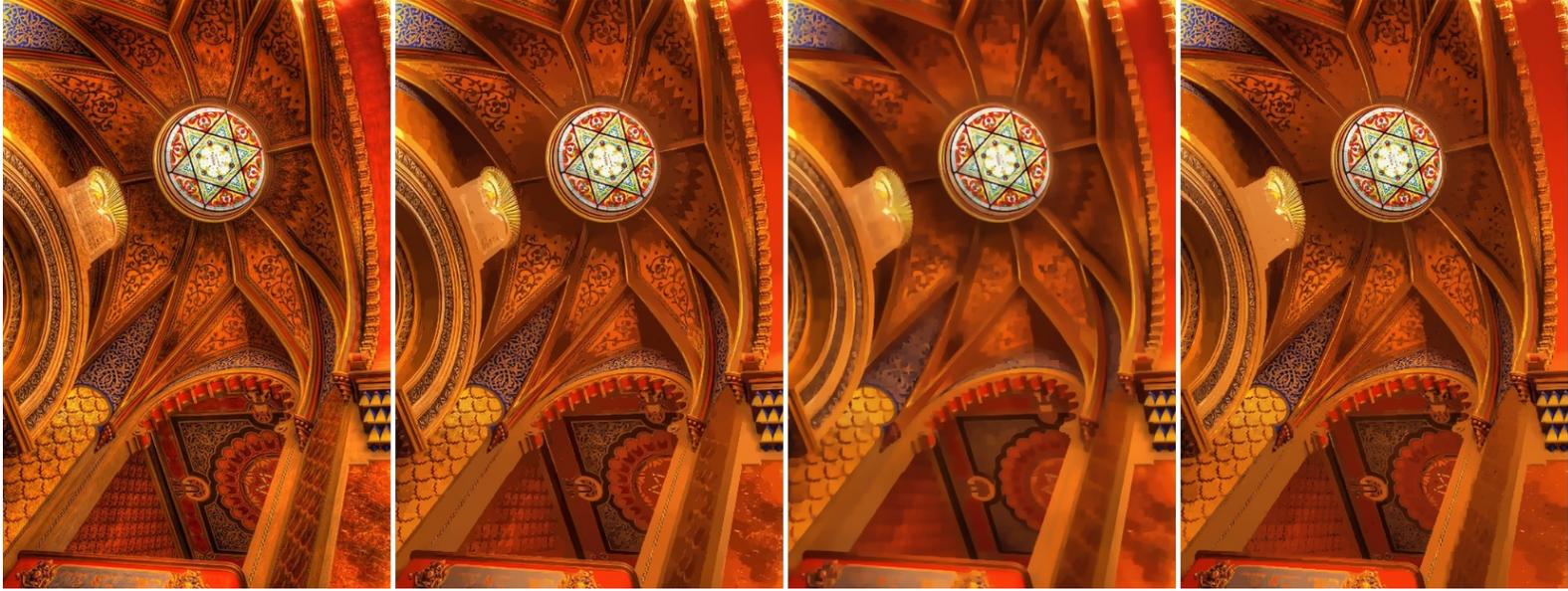
L1 (repeat 10 times)

(default official parameters)

(default official parameters)

(default official parameters)

Figure 10: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.



Source

L0

RTV

L1

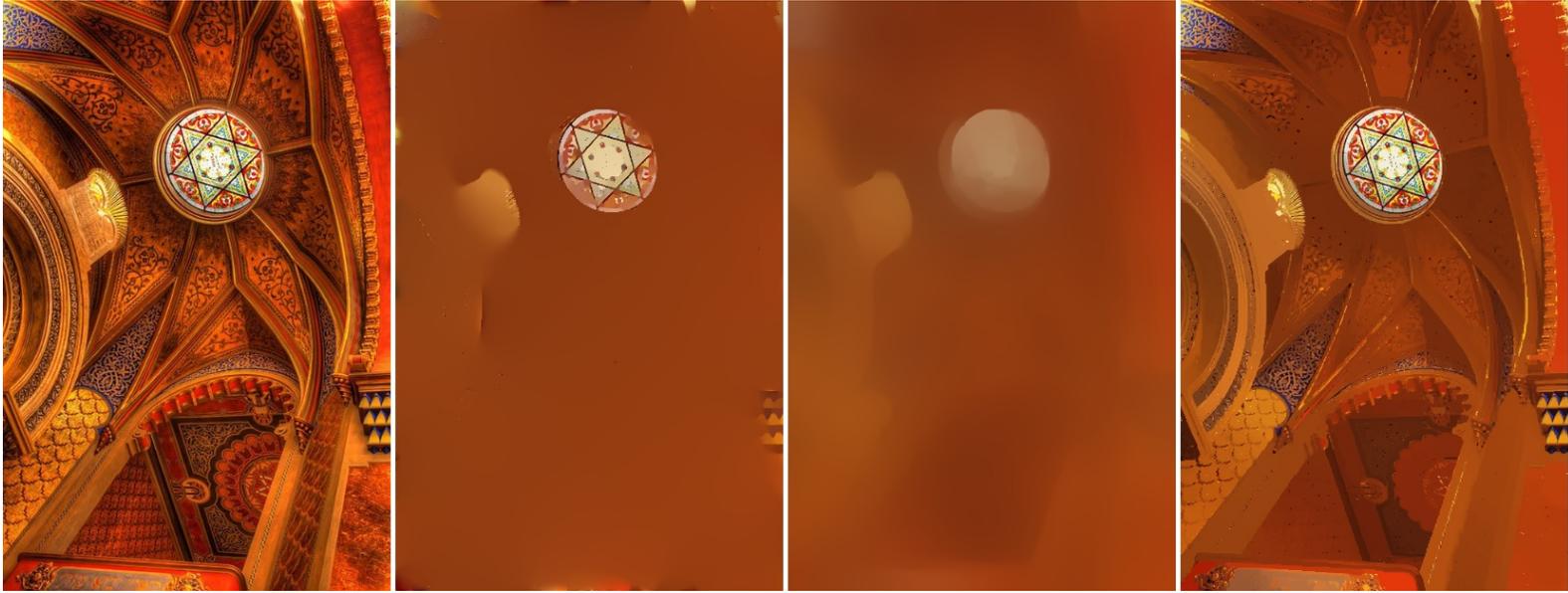


EAP + L0

EAP + RTV

EAP + L1

Figure 11: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.



Source

L0 (extreme parameter  $\lambda=0.1$ ) RTV (extreme parameter  $\lambda=0.2$ ) L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)

RTV (repeat 10 times)

L1 (repeat 10 times)

(default official parameters)

(default official parameters)

(default official parameters)

Figure 12: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.

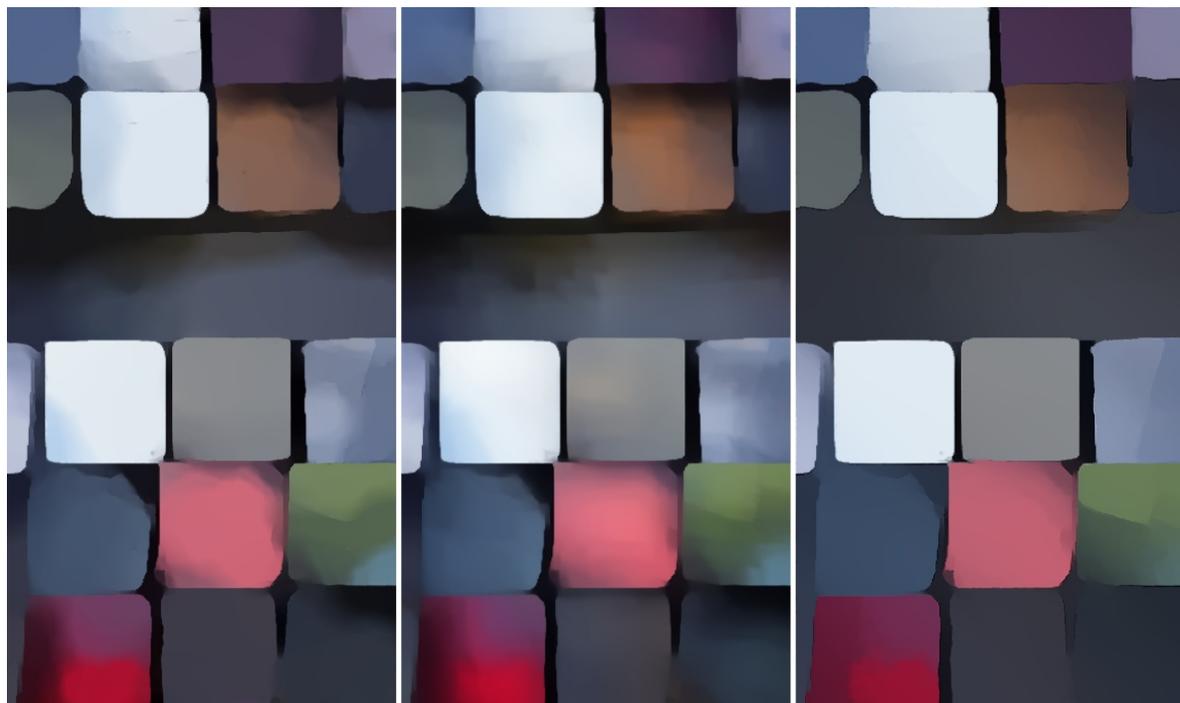


Source

L0

RTV

L1



EAP + L0

EAP + RTV

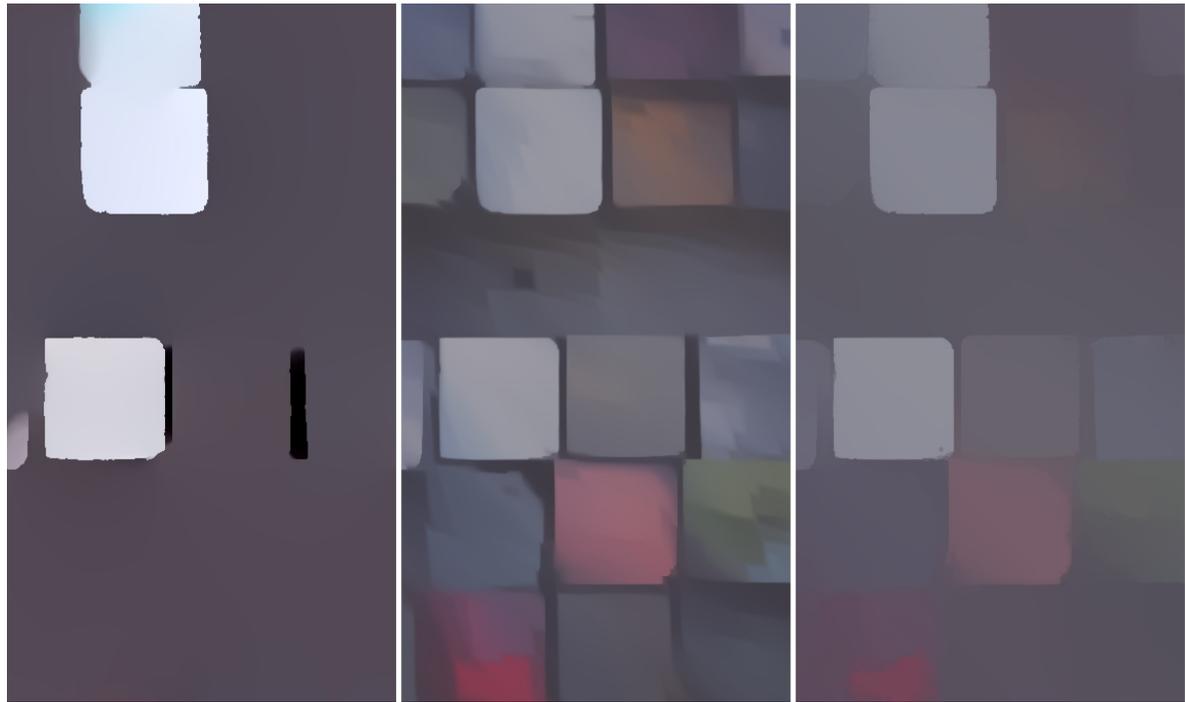
EAP + L1

Figure 13: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.



Source

L0 (extreme parameter  $\lambda=0.1$ ) RTV (extreme parameter  $\lambda=0.2$ ) L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)

RTV (repeat 10 times)

L1 (repeat 10 times)

(default official parameters)

(default official parameters)

(default official parameters)

Figure 14: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.



Source

L0

RTV

L1

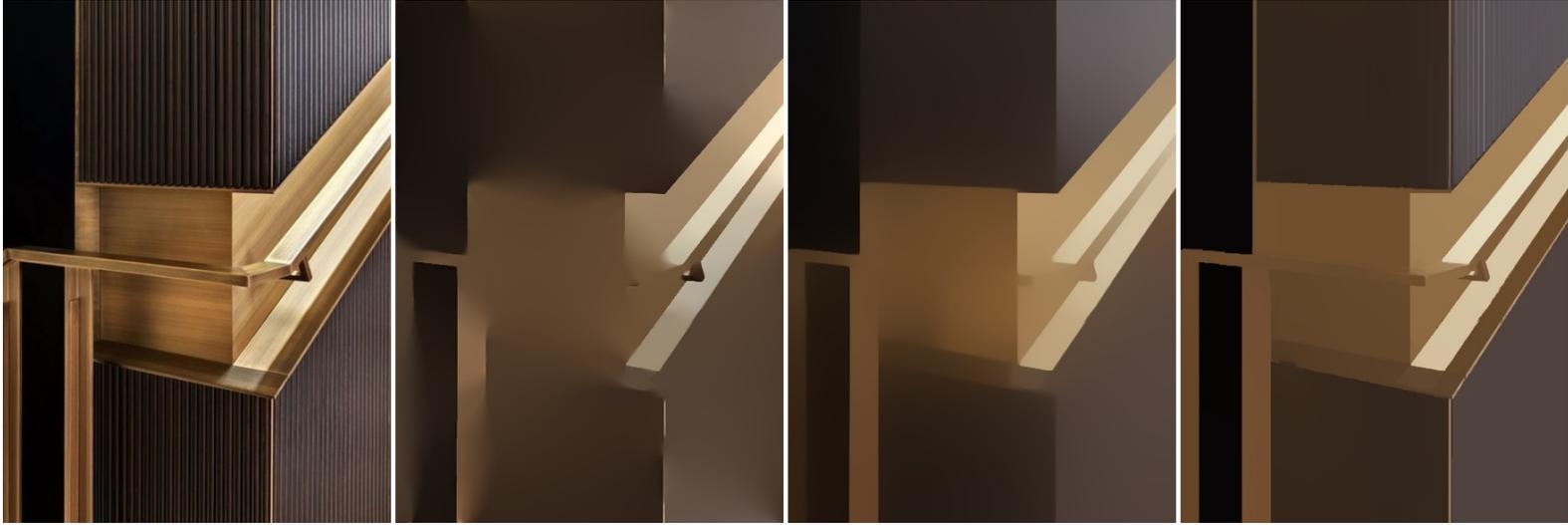


EAP + L0

EAP + RTV

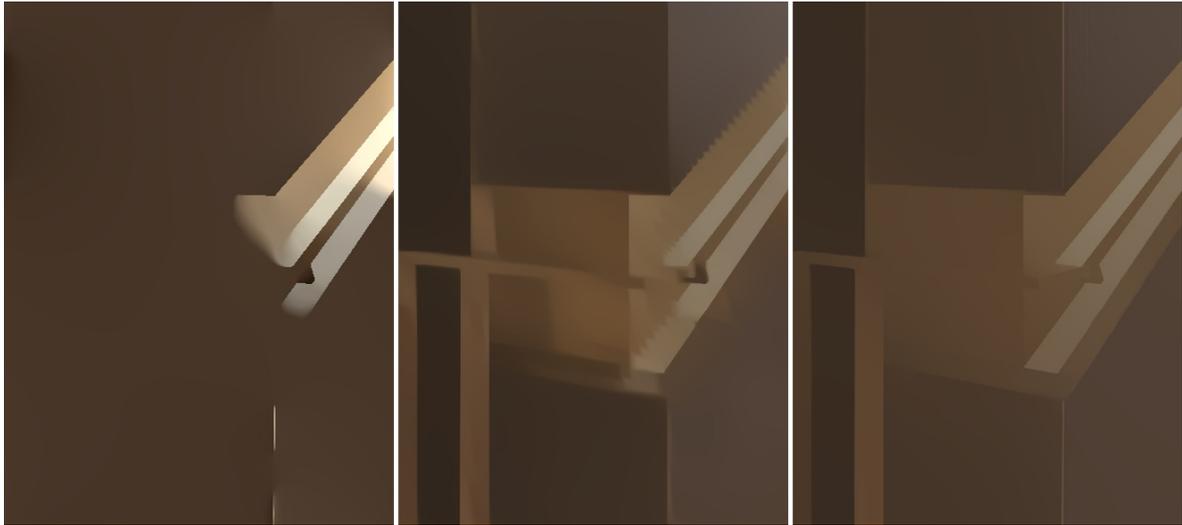
EAP + L1

Figure 15: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.



Source

L0 (extreme parameter  $\lambda=0.1$ ) RTV (extreme parameter  $\lambda=0.2$ ) L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)

RTV (repeat 10 times)

L1 (repeat 10 times)

(default official parameters)

(default official parameters)

(default official parameters)

Figure 16: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.



Source

L0

RTV

L1



EAP + L0

EAP + RTV

EAP + L1

Figure 17: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.



Source

L0 (extreme parameter  $\lambda=0.1$ ) RTV (extreme parameter  $\lambda=0.2$ ) L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)

RTV (repeat 10 times)

L1 (repeat 10 times)

(default official parameters)

(default official parameters)

(default official parameters)

Figure 18: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.

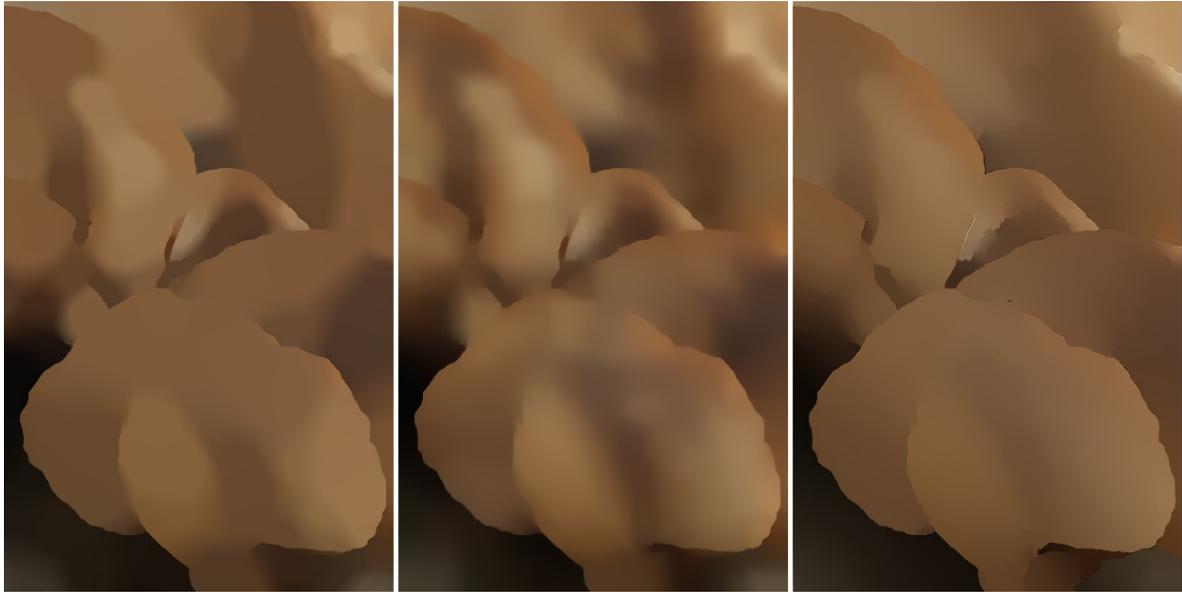


Source

L0

RTV

L1

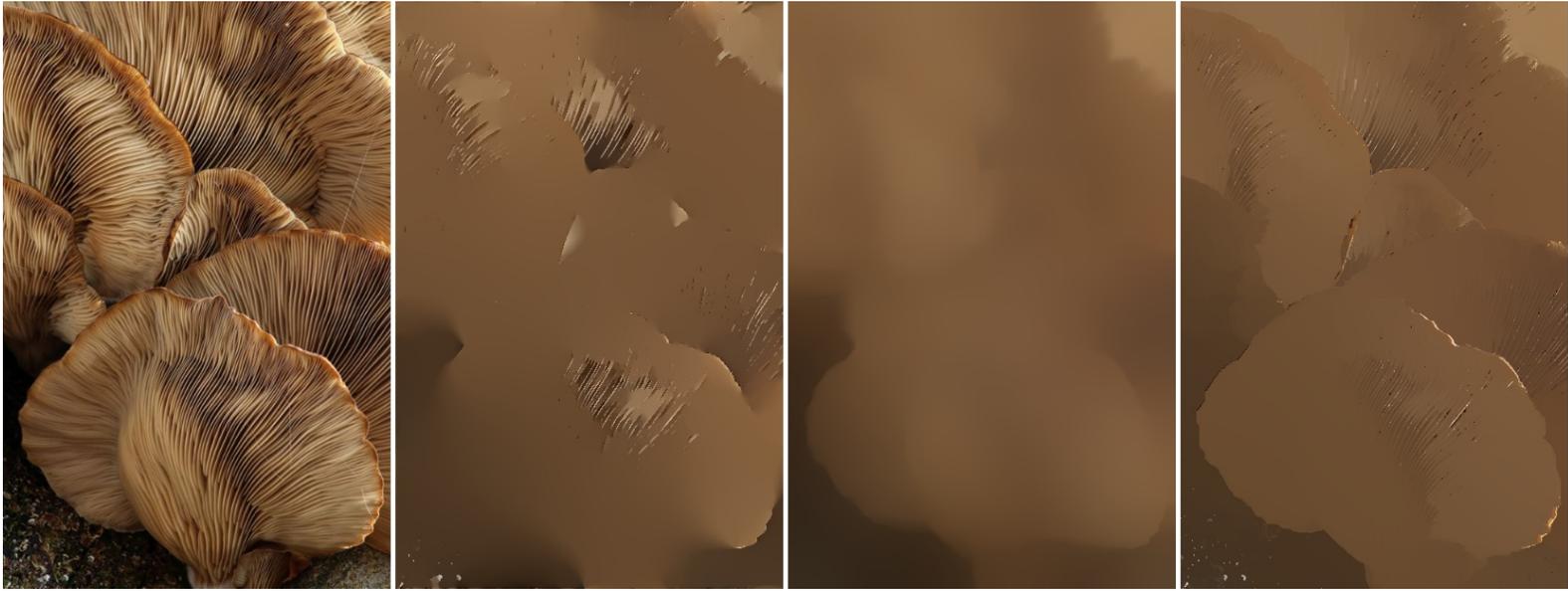


EAP + L0

EAP + RTV

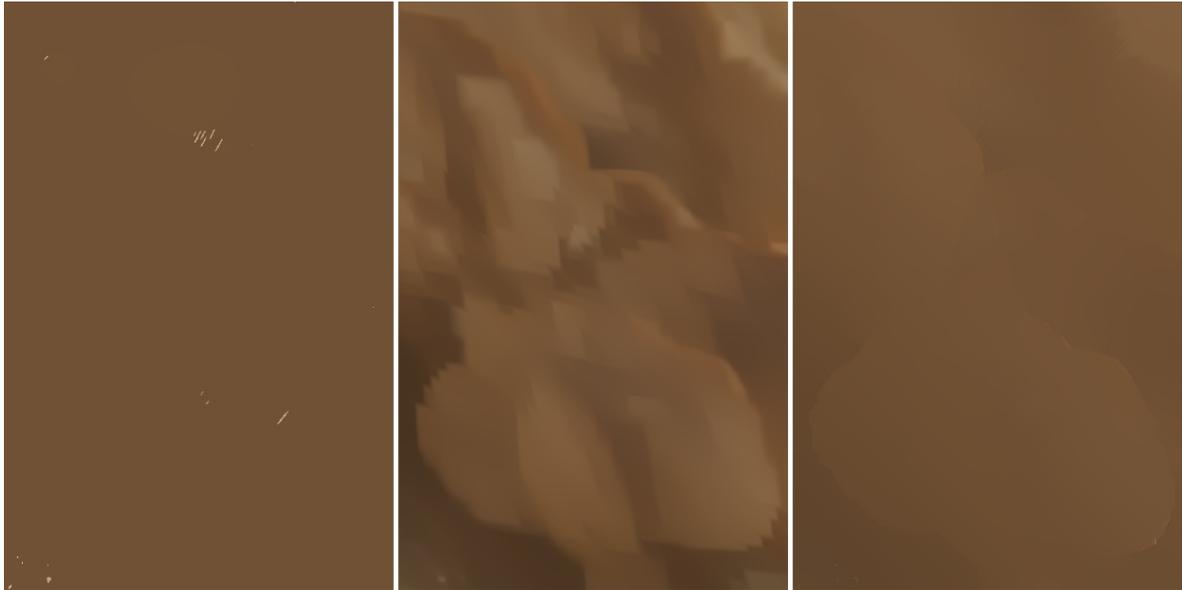
EAP + L1

Figure 19: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.



Source

L0 (extreme parameter  $\lambda=0.1$ ) RTV (extreme parameter  $\lambda=0.2$ ) L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)

RTV (repeat 10 times)

L1 (repeat 10 times)

(default official parameters)

(default official parameters)

(default official parameters)

Figure 20: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.

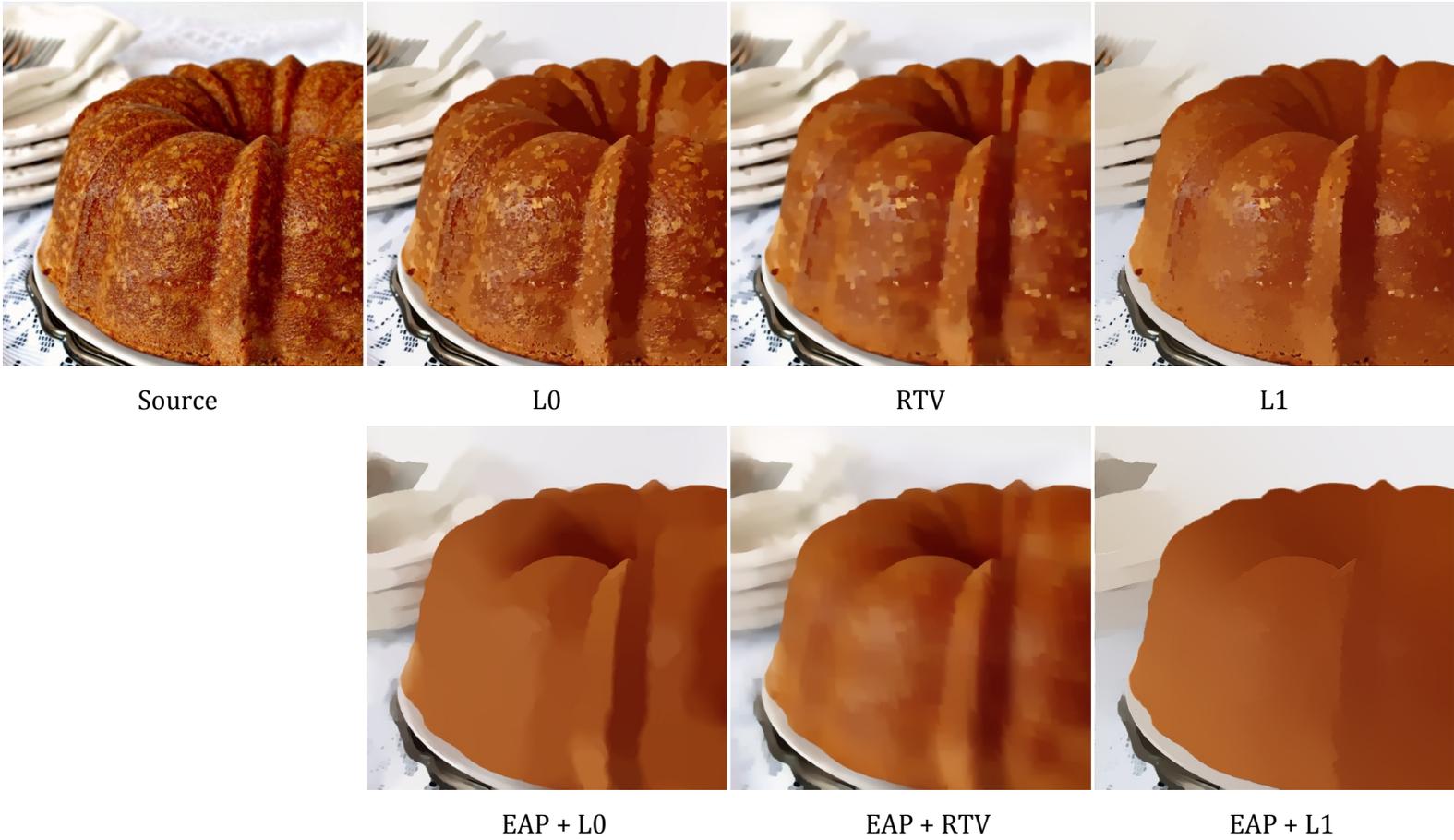


Figure 21: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.

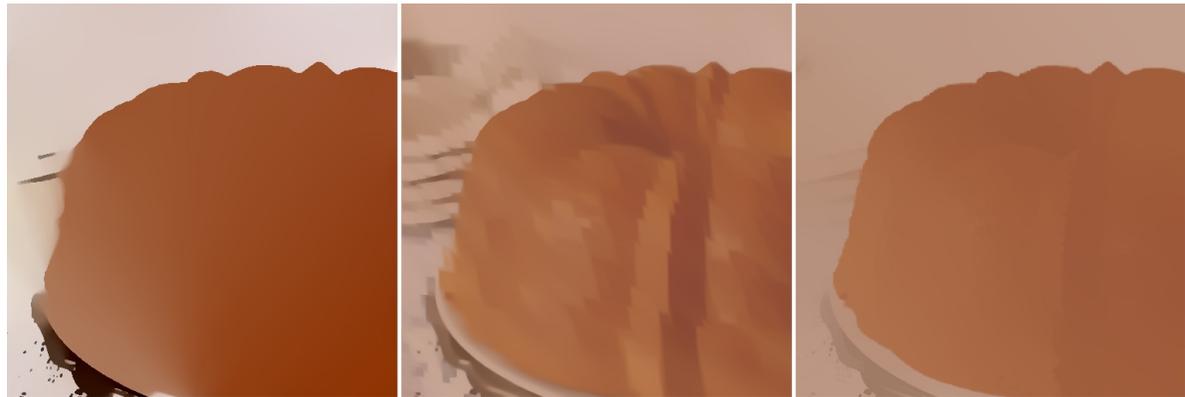


Source

L0 (extreme parameter  $\lambda=0.1$ )

RTV (extreme parameter  $\lambda=0.2$ )

L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)

RTV (repeat 10 times)

L1 (repeat 10 times)

(default official parameters)

(default official parameters)

(default official parameters)

Figure 22: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.

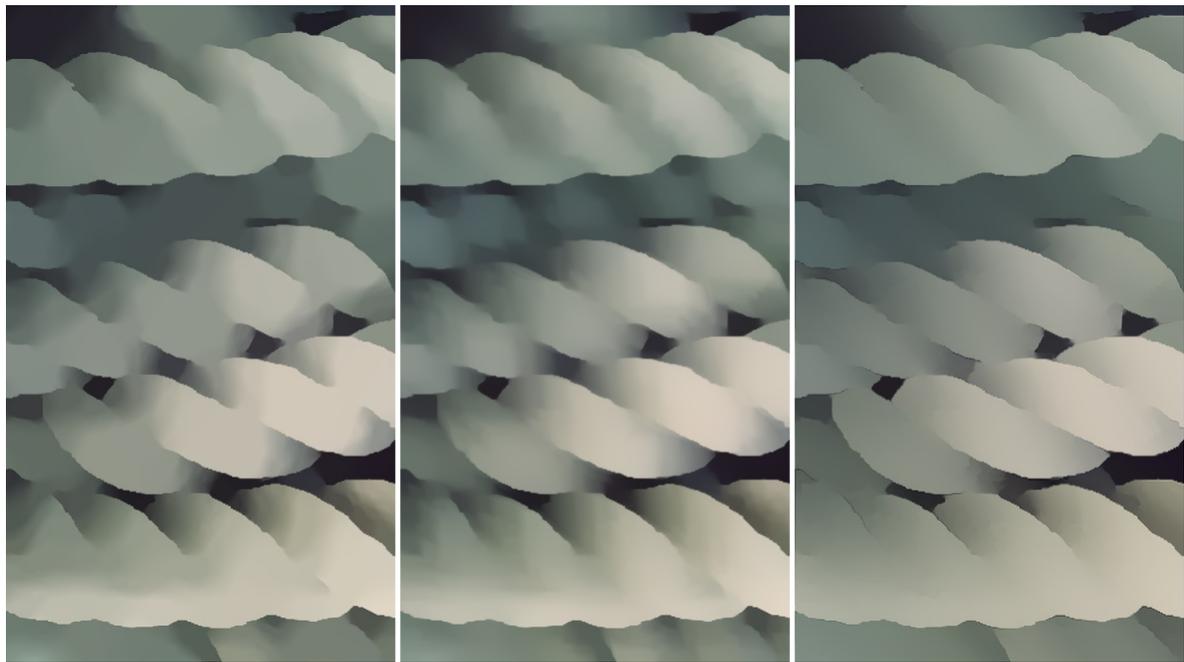


Source

L0

RTV

L1



EAP + L0

EAP + RTV

EAP + L1

Figure 23: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.



Source



L0 (extreme parameter  $\lambda=0.1$ )



RTV (extreme parameter  $\lambda=0.2$ )



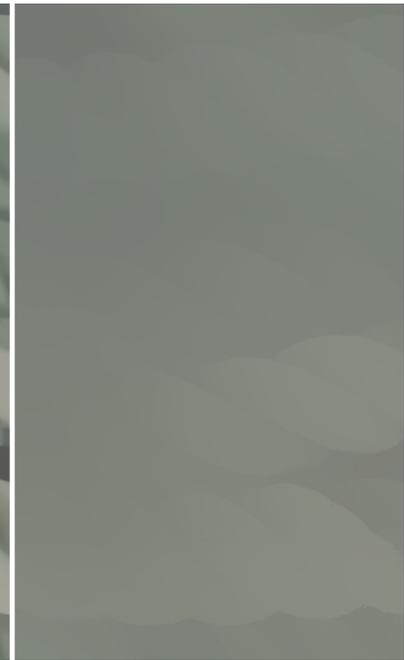
L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)  
(default official parameters)



RTV (repeat 10 times)  
(default official parameters)



L1 (repeat 10 times)  
(default official parameters)

Figure 24: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.

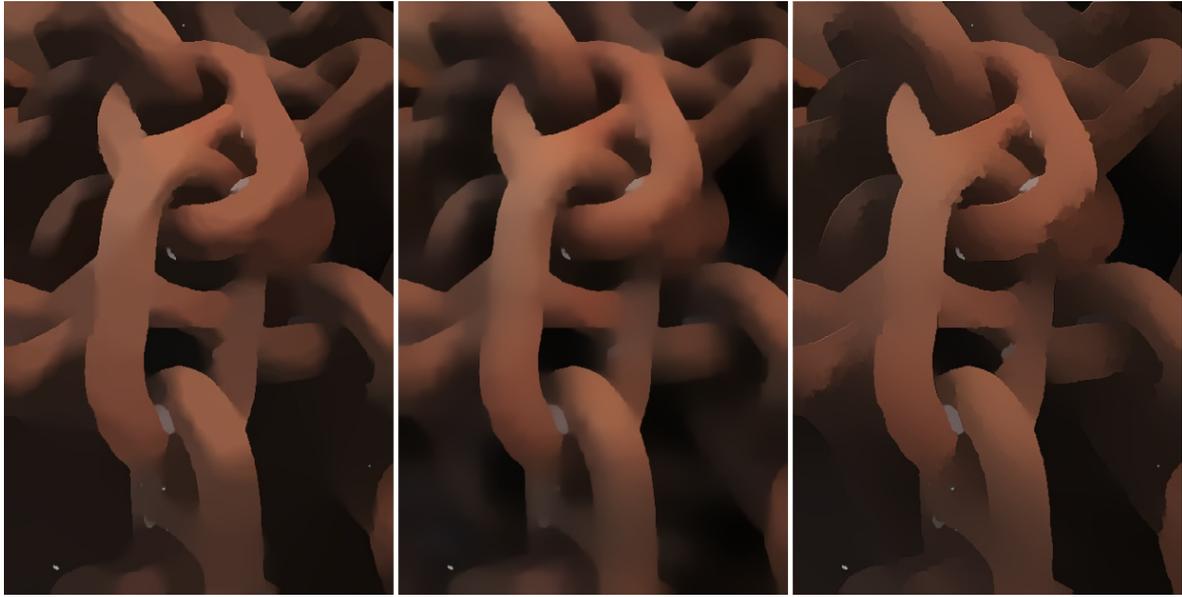


Source

L0

RTV

L1

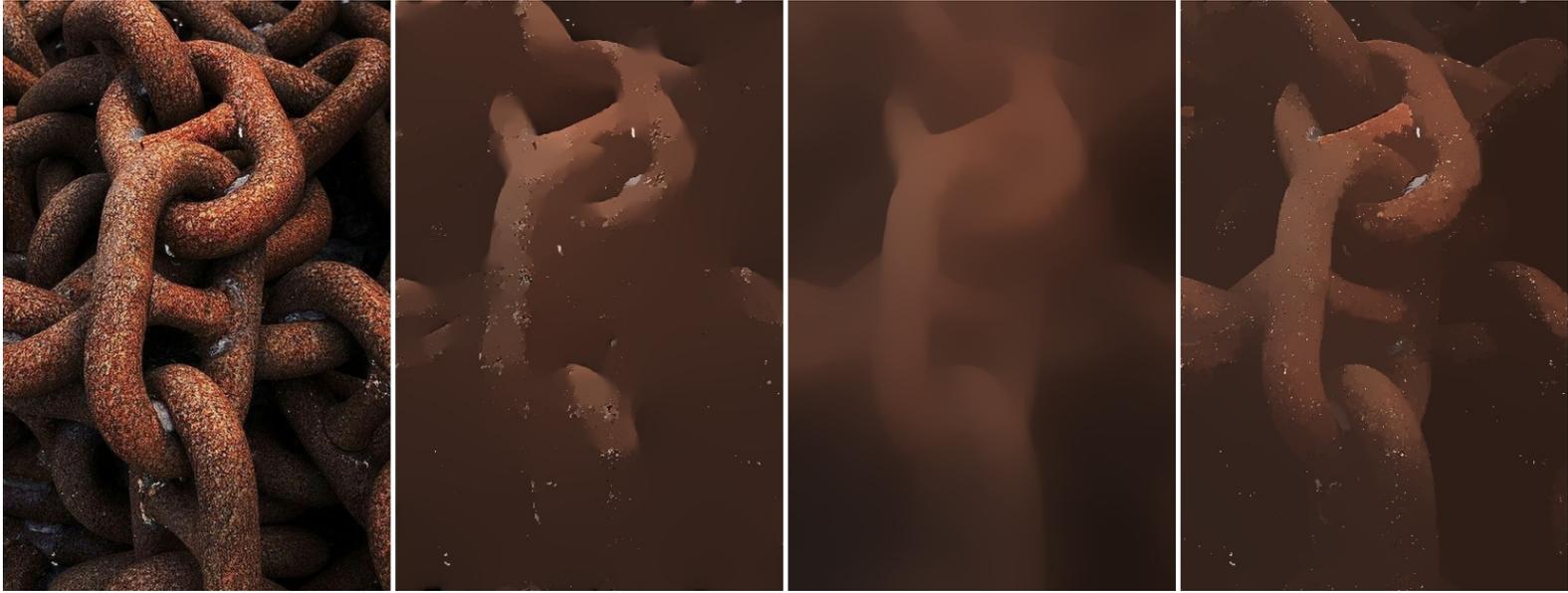


EAP + L0

EAP + RTV

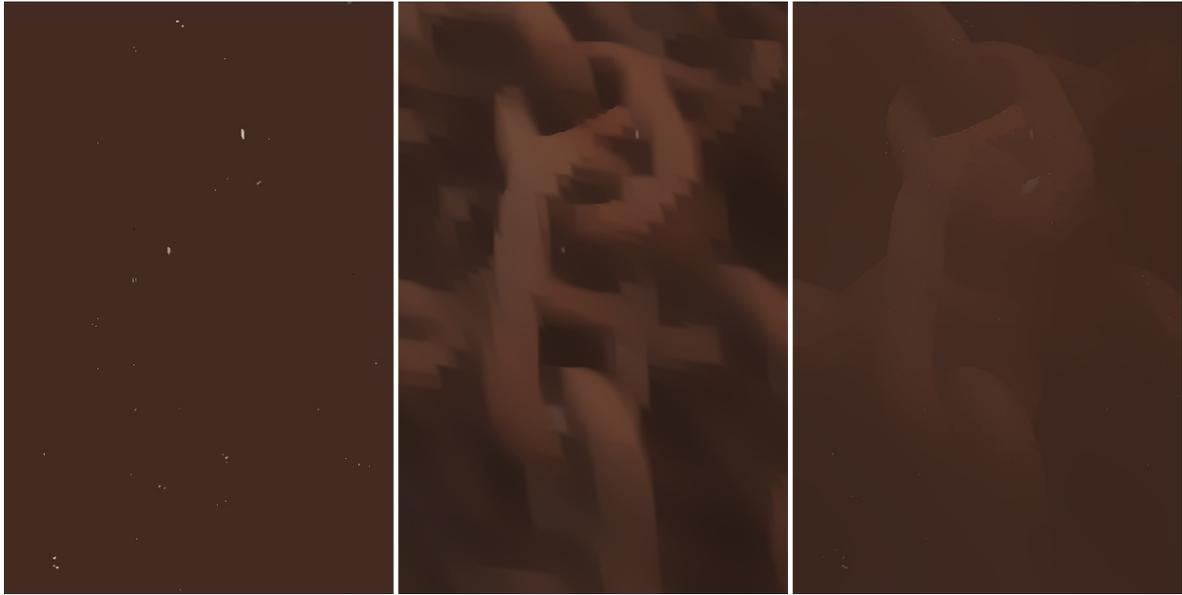
EAP + L1

Figure 25: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.



Source

L0 (extreme parameter  $\lambda=0.1$ ) RTV (extreme parameter  $\lambda=0.2$ ) L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)

RTV (repeat 10 times)

L1 (repeat 10 times)

(default official parameters)

(default official parameters)

(default official parameters)

Figure 26: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.



Source

L0

RTV

L1

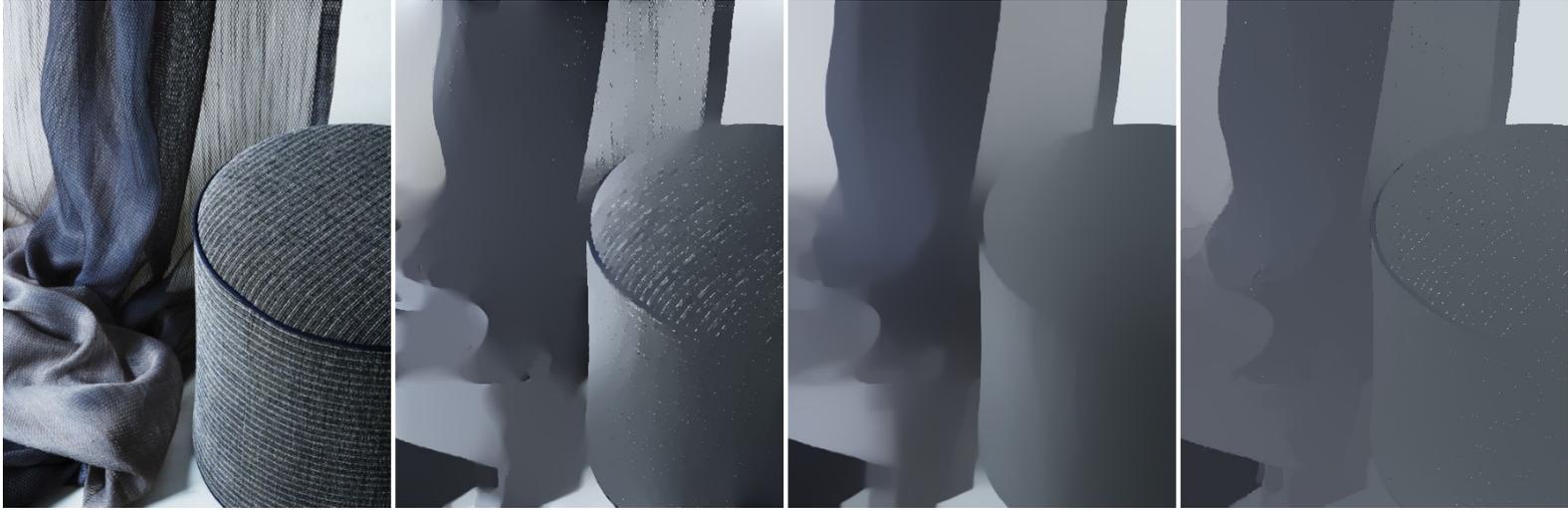


EAP + L0

EAP + RTV

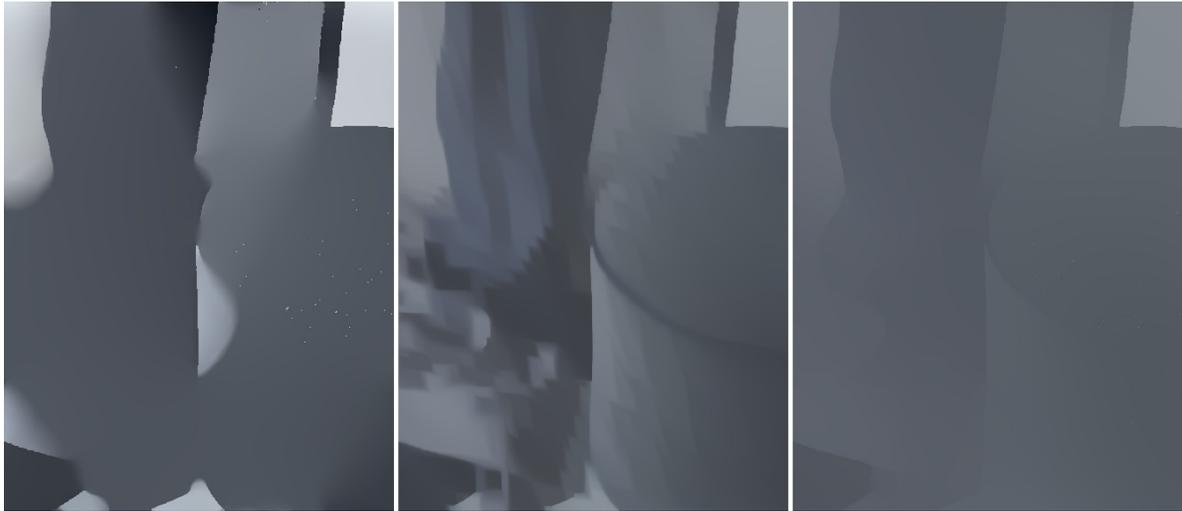
EAP + L1

Figure 27: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.



Source

L0 (extreme parameter  $\lambda=0.1$ ) RTV (extreme parameter  $\lambda=0.2$ ) L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)

RTV (repeat 10 times)

L1 (repeat 10 times)

(default official parameters)

(default official parameters)

(default official parameters)

Figure 28: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.



Source

L0

RTV

L1



EAP + L0

EAP + RTV

EAP + L1

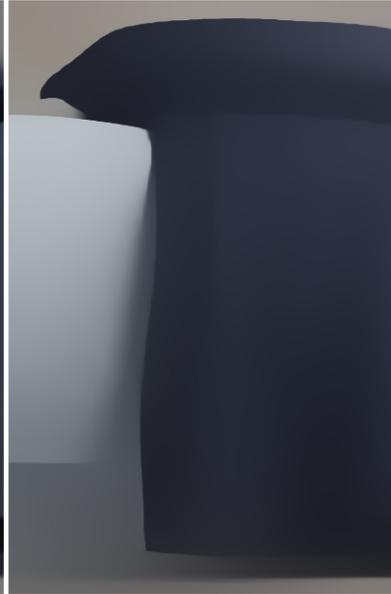
Figure 29: **Texture removal.** Visual comparison of texture removal with or without the EAP framework.



Source



L0 (extreme parameter  $\lambda=0.1$ )



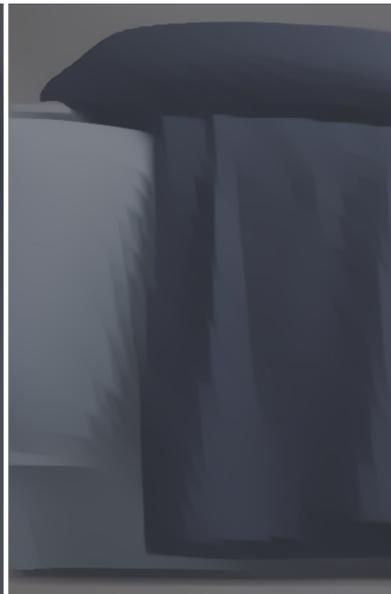
RTV (extreme parameter  $\lambda=0.2$ )



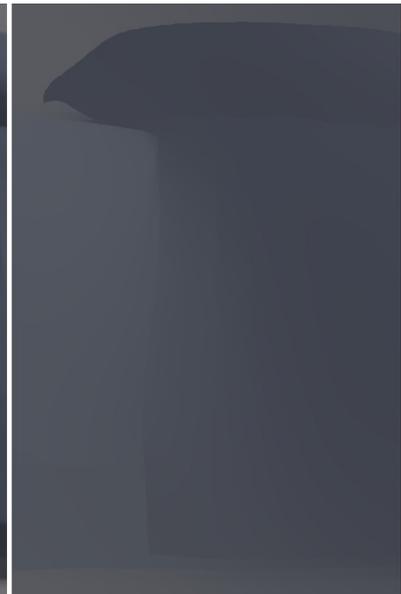
L1 (extreme parameter  $\lambda=5$ )



L0 (repeat 10 times)  
(default official parameters)

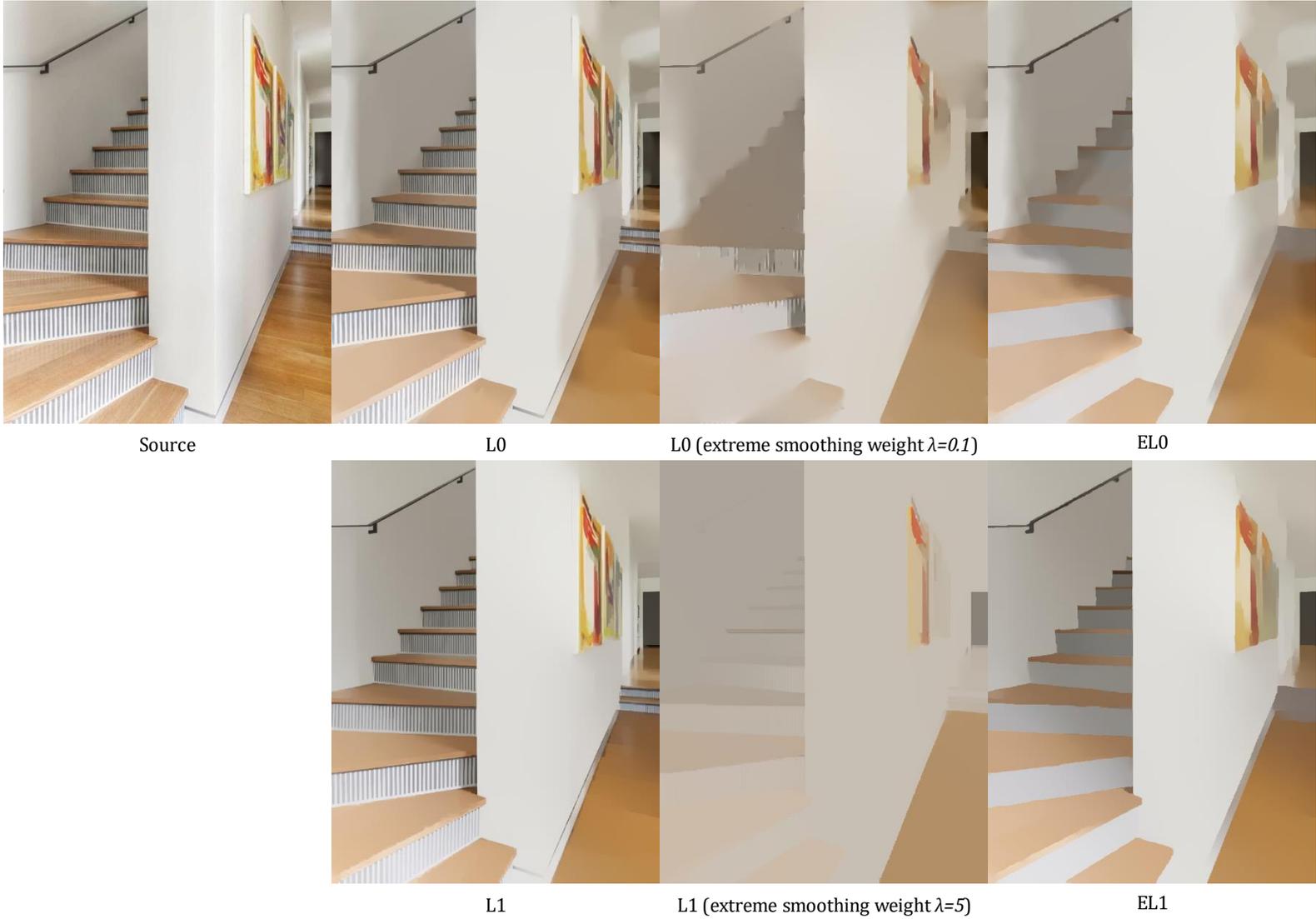


RTV (repeat 10 times)  
(default official parameters)



L1 (repeat 10 times)  
(default official parameters)

Figure 30: **Texture removal.** Trying to fine tune existing methods to facilitate adequate smoothing. The EAP results cannot be achieved by tuning parameters of existing methods or repeating existing methods for multiple times.



Source

L0

L0 (extreme smoothing weight  $\lambda=0.1$ )

EL0

L1

L1 (extreme smoothing weight  $\lambda=5$ )

EL1

Figure 31: **Texture removal.** The visual effect of EAP cannot be achieved by tuning smoothing parameters of previous methods. We provide several smoothed results using previous methods and extreme parameters. The EAP achieves results significantly better than that from extremely tuned previous methods.



Source



DL1



DL1(shadow)



DL1(specular reflection)



EDL1



EDL1(shadow)



EDL1(specular reflection)

Figure 32: **Layer decomposition.** Visual comparison of layer decomposition with or without the EAP framework.

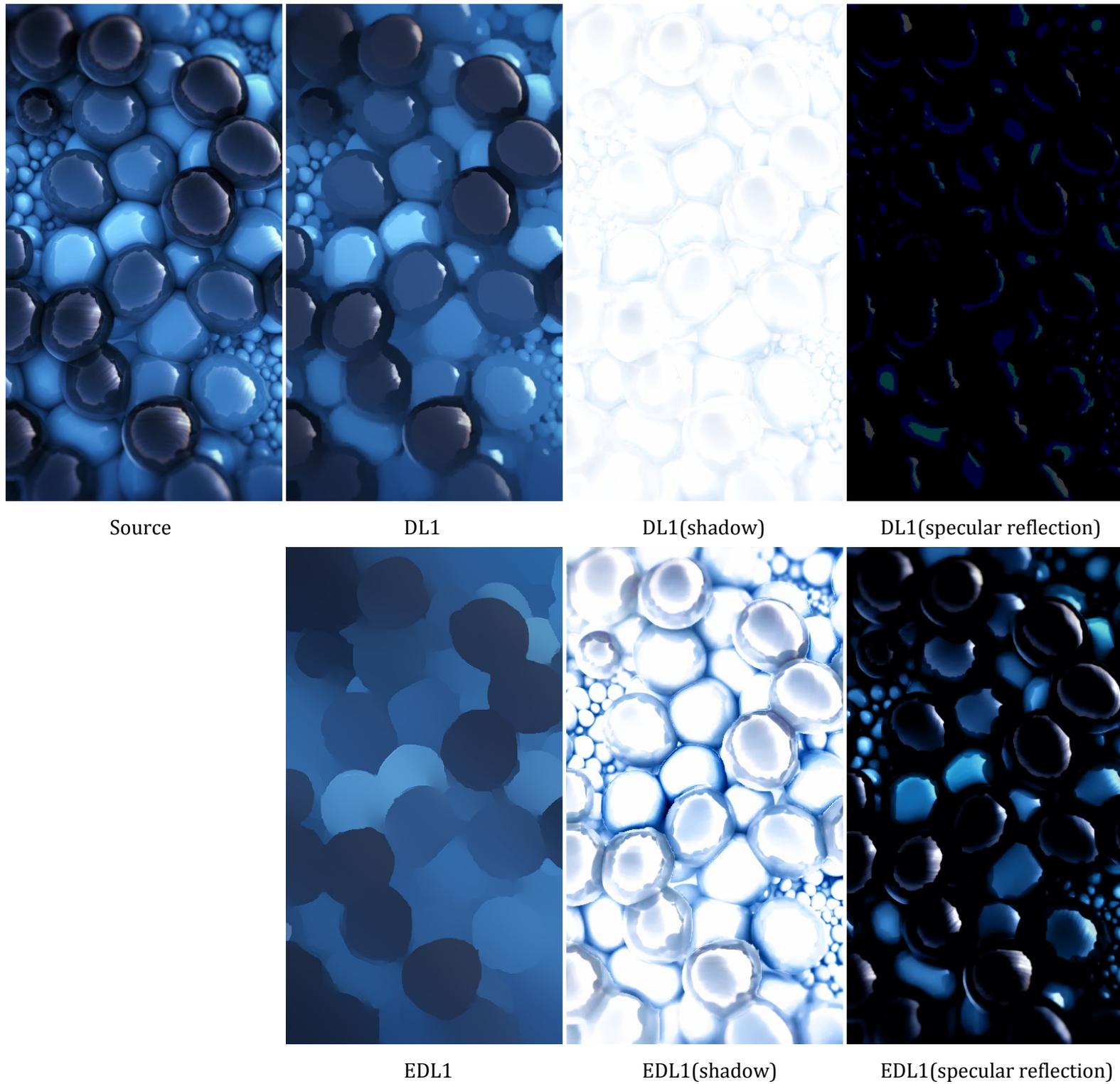


Figure 33: **Layer decomposition.** Visual comparison of layer decomposition with or without the EAP framework.

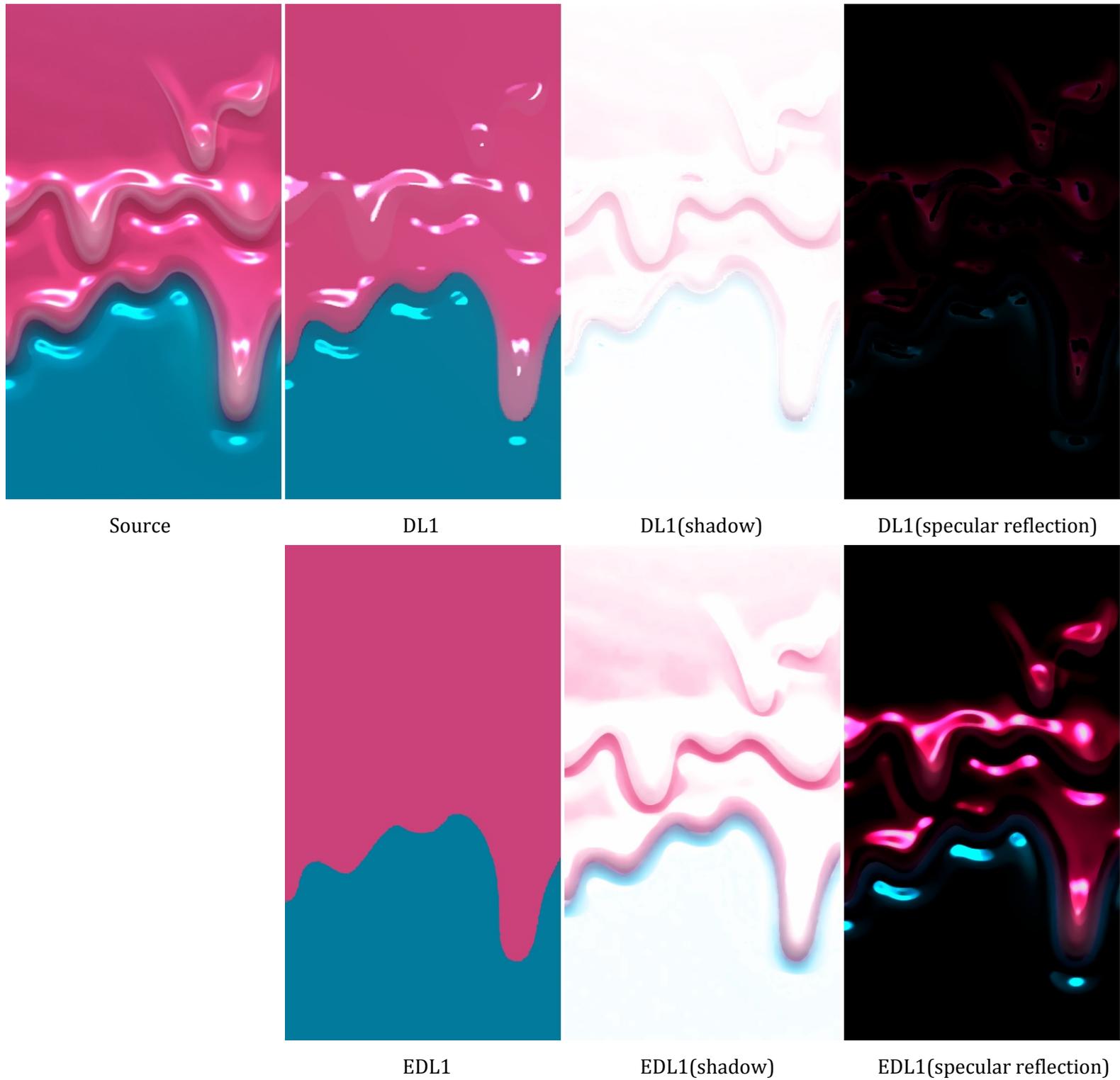


Figure 34: **Layer decomposition.** Visual comparison of layer decomposition with or without the EAP framework.



Source



DL1



DL1(shadow)



DL1(specular reflection)



EDL1



EDL1(shadow)



EDL1(specular reflection)

Figure 35: **Layer decomposition.** Visual comparison of layer decomposition with or without the EAP framework.



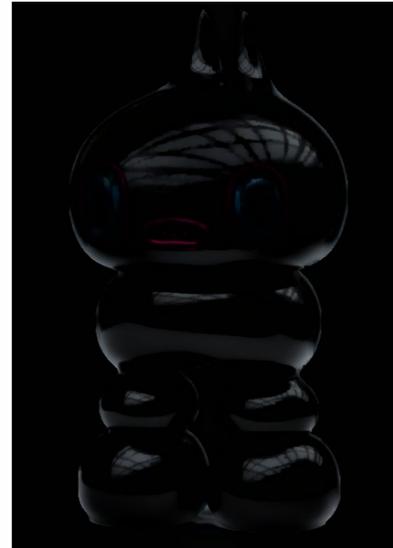
Source



DL1



DL1(shadow)



DL1(specular reflection)



EDL1

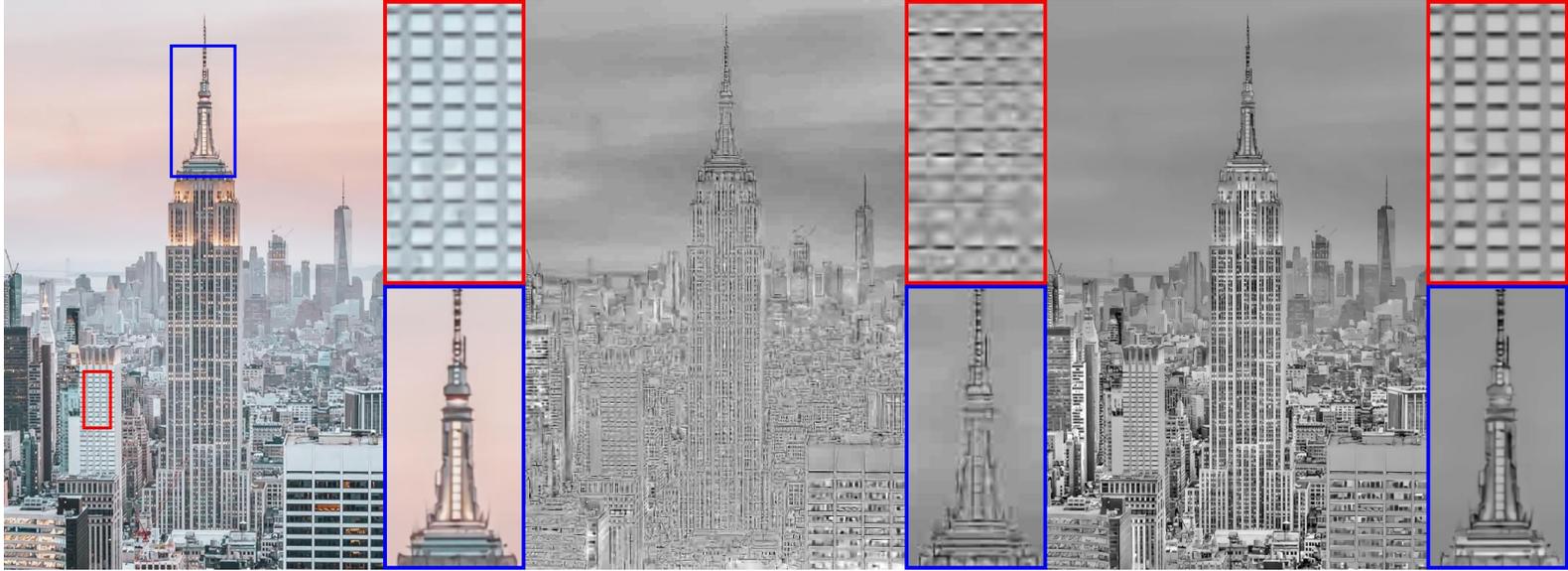


EDL1(shadow)



EDL1(specular reflection)

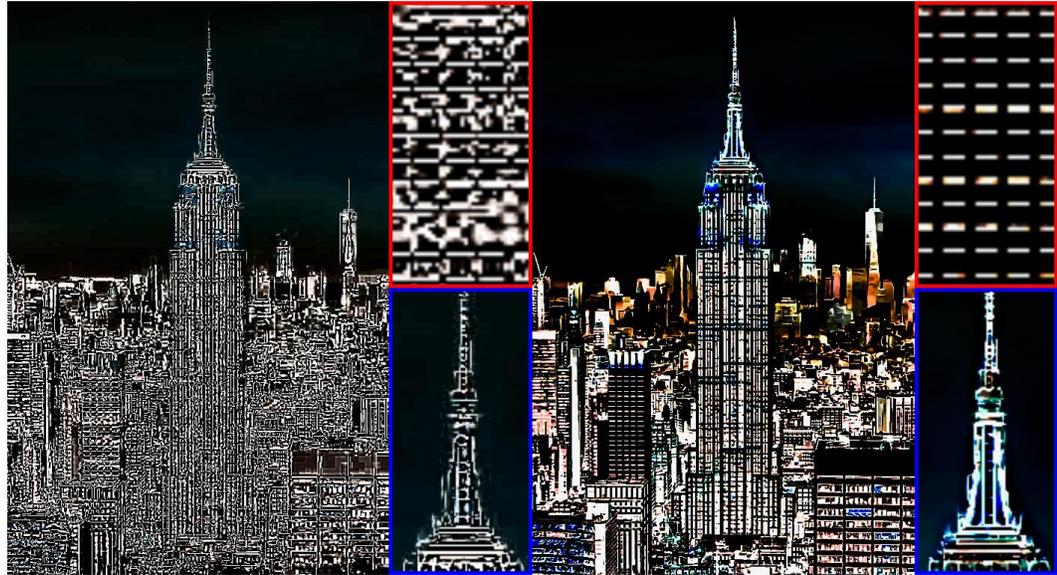
Figure 36: **Layer decomposition.** Visual comparison of layer decomposition with or without the EAP framework.



Source

DL1(shading)

EDL1(shading)



DL1(shading inverted)

EDL1(shading inverted)

Figure 37: **Illumination manipulation.** Visual comparison of gamma corrected shading map inverting with or without the EAP framework.

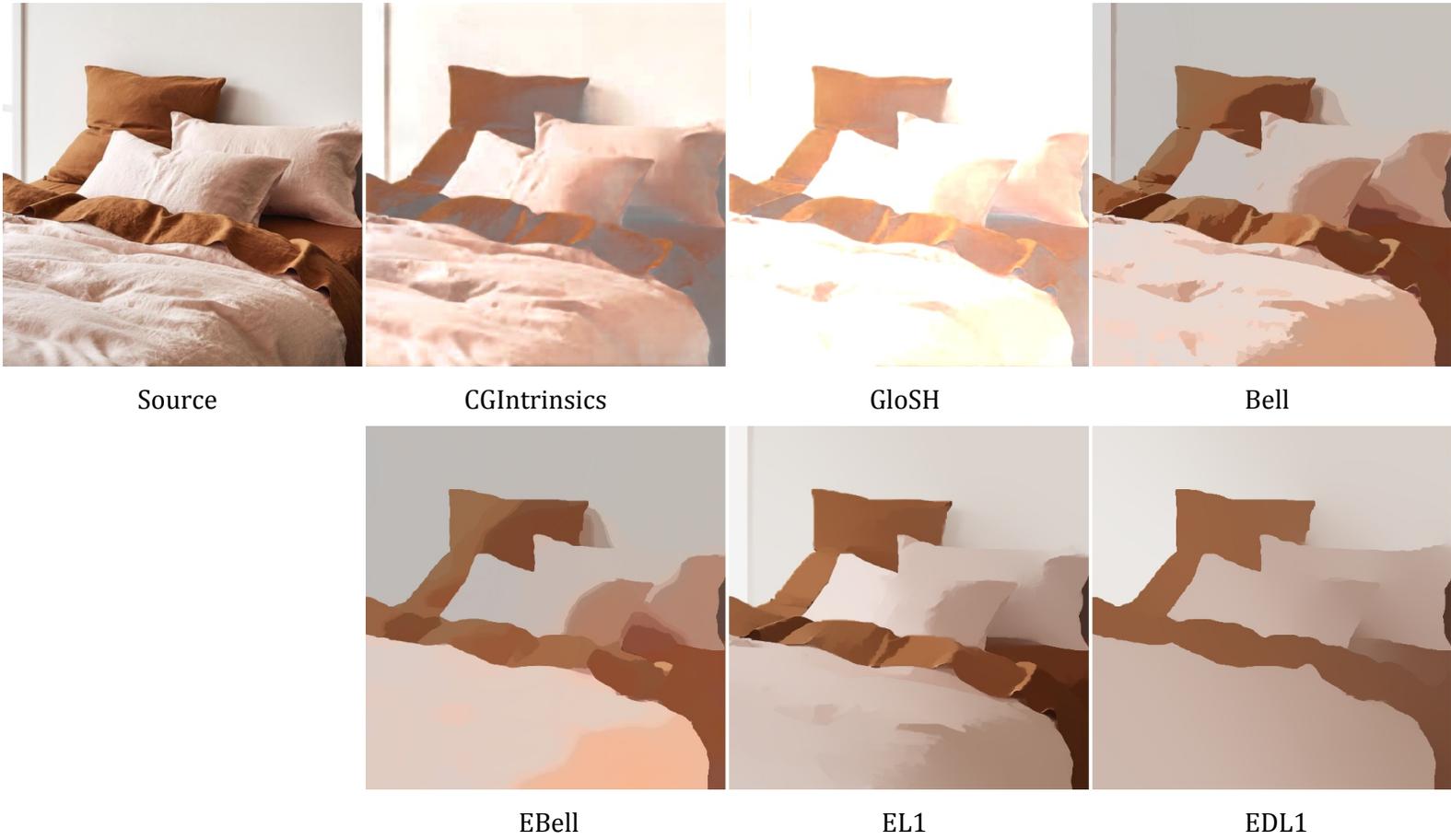
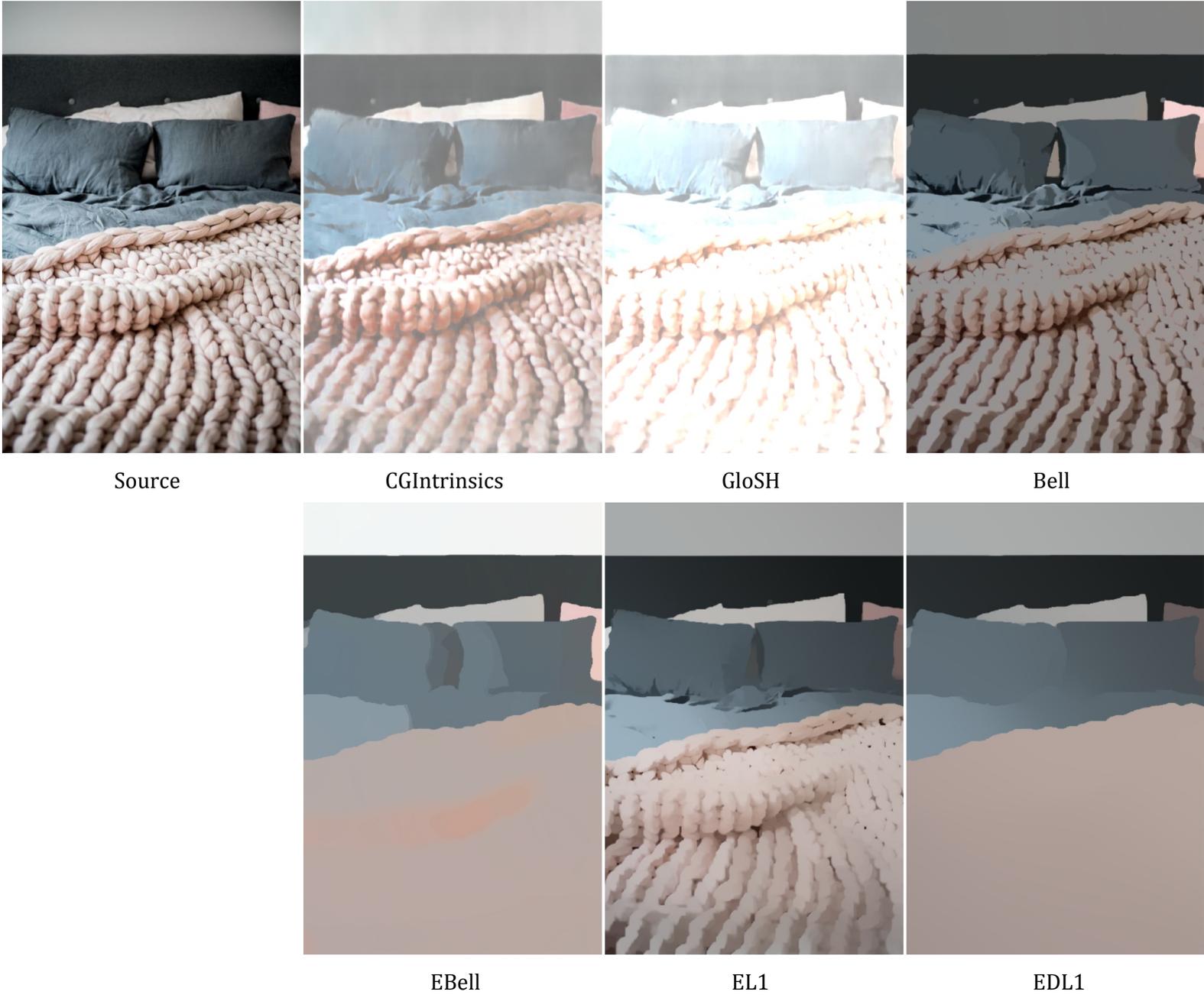


Figure 38: **Intrinsic decomposition.** Visual comparison of intrinsic reflectance extraction with or without the EAP framework, **without** hue/saturation constraint. (The reflectance is **not** required to have same pixel hue and saturation with source images.)



Figure 39: **Intrinsic decomposition.** Visual comparison of intrinsic reflectance extraction with or without the EAP framework, **with** hue/saturation constraint. (The reflectance is required to have same pixel hue and saturation with source images. The hue and saturation channels in all reflectance maps are replaced by the original hue and saturation in the source image.)



Source

CGIntrinsics

GloSH

Bell

EBell

EL1

EDL1

Figure 40: **Intrinsic decomposition.** Visual comparison of intrinsic reflectance extraction with or without the EAP framework, **without** hue/saturation constraint. (The reflectance is **not** required to have same pixel hue and saturation with source images.)

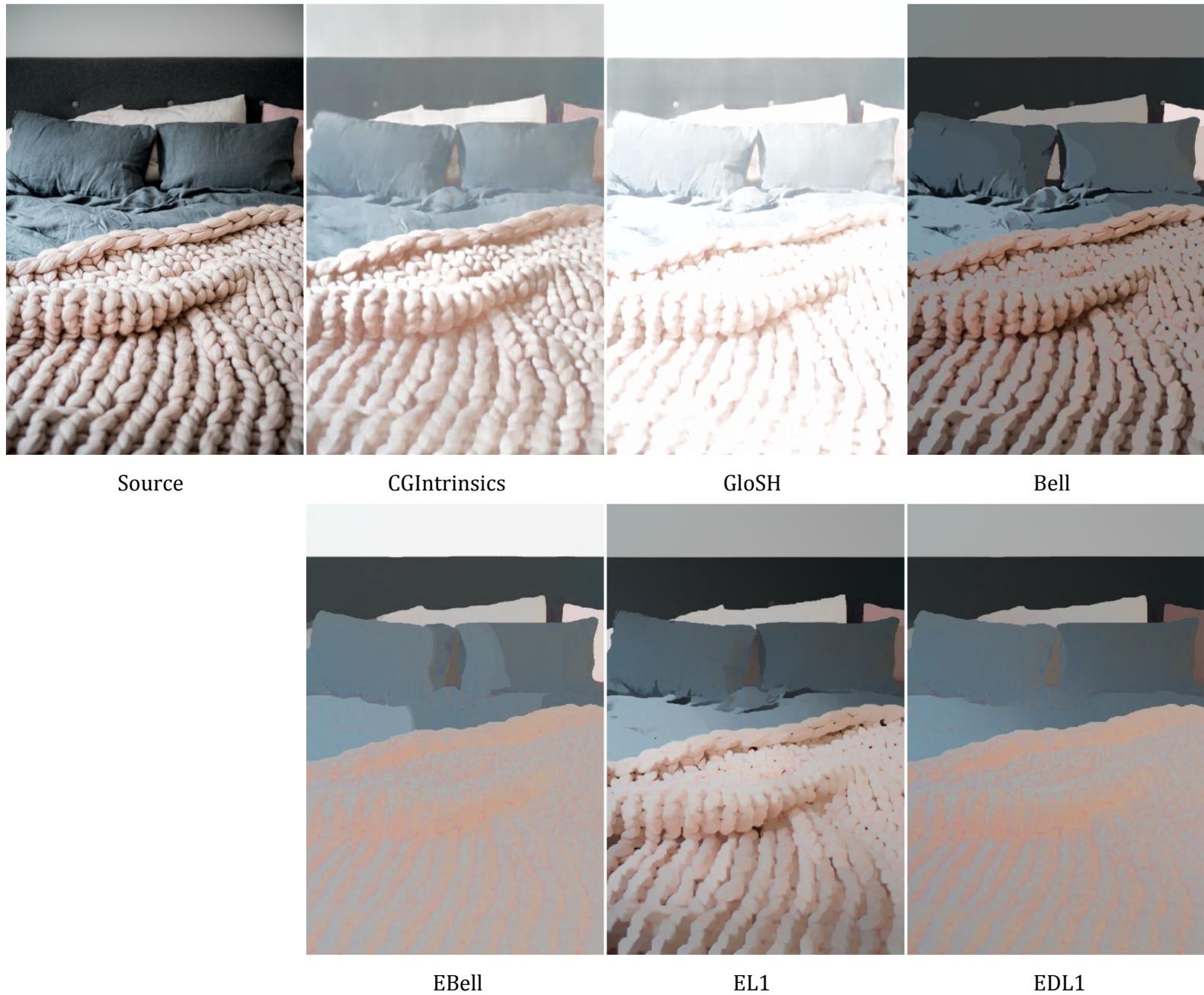


Figure 41: **Intrinsic decomposition.** Visual comparison of intrinsic reflectance extraction with or without the EAP framework, **with** hue/saturation constraint. (The reflectance is required to have same pixel hue and saturation with source images. The hue and saturation channels in all reflectance maps are replaced by the original hue and saturation in the source image.)



Source



CGIntrinsics



GloSH



Bell



DL1



EBell



EDL1

Figure 42: **Specular reflection removal.** Visual comparison of specular reflection removal using different intrinsic decomposition methods.



Source

CGIntrinsics

GloSH

Bell



DL1

EBell

EDL1

Figure 43: **Specular reflection removal.** Visual comparison of specular reflection removal using different intrinsic decomposition methods.



Source



CGIntrinsics



GloSH



Bell



DL1



EBell



EDL1

Figure 44: **Specular reflection removal.** Visual comparison of specular reflection removal using different intrinsic decomposition methods.



Source



CGIntrinsics



GloSH



Bell



DL1



EBell



EDL1

Figure 45: **Specular reflection removal.** Visual comparison of specular reflection removal using different intrinsic decomposition methods.



Source



CGIntrinsics



GloSH



Bell



DL1



EBell



EDL1

Figure 46: **Specular reflection removal.** Visual comparison of specular reflection removal using different intrinsic decomposition methods.



Source

CGIntrinsics

GloSH

Bell



DL1

EBell

EDL1

Figure 47: **Specular reflection removal.** Visual comparison of specular reflection removal using different intrinsic decomposition methods.



Source



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Bell



DL1



EBell



EDL1

Figure 48: **Specular reflection removal.** Visual comparison of specular reflection removal using different intrinsic decomposition methods.



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GloSH

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DL1

EBell

EDL1

Figure 49: **Specular reflection removal.** Visual comparison of specular reflection removal using different intrinsic decomposition methods.



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DL1

EBell

EDL1

Figure 50: **Specular reflection removal.** Visual comparison of specular reflection removal using different intrinsic decomposition methods.



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DL1

EBell

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Figure 51: **Specular reflection removal.** Visual comparison of specular reflection removal using different intrinsic decomposition methods.



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DL1

NBell

ND1

Figure 52: **Specular reflection removal.** Visual comparison of specular reflection removal using different intrinsic decomposition methods.



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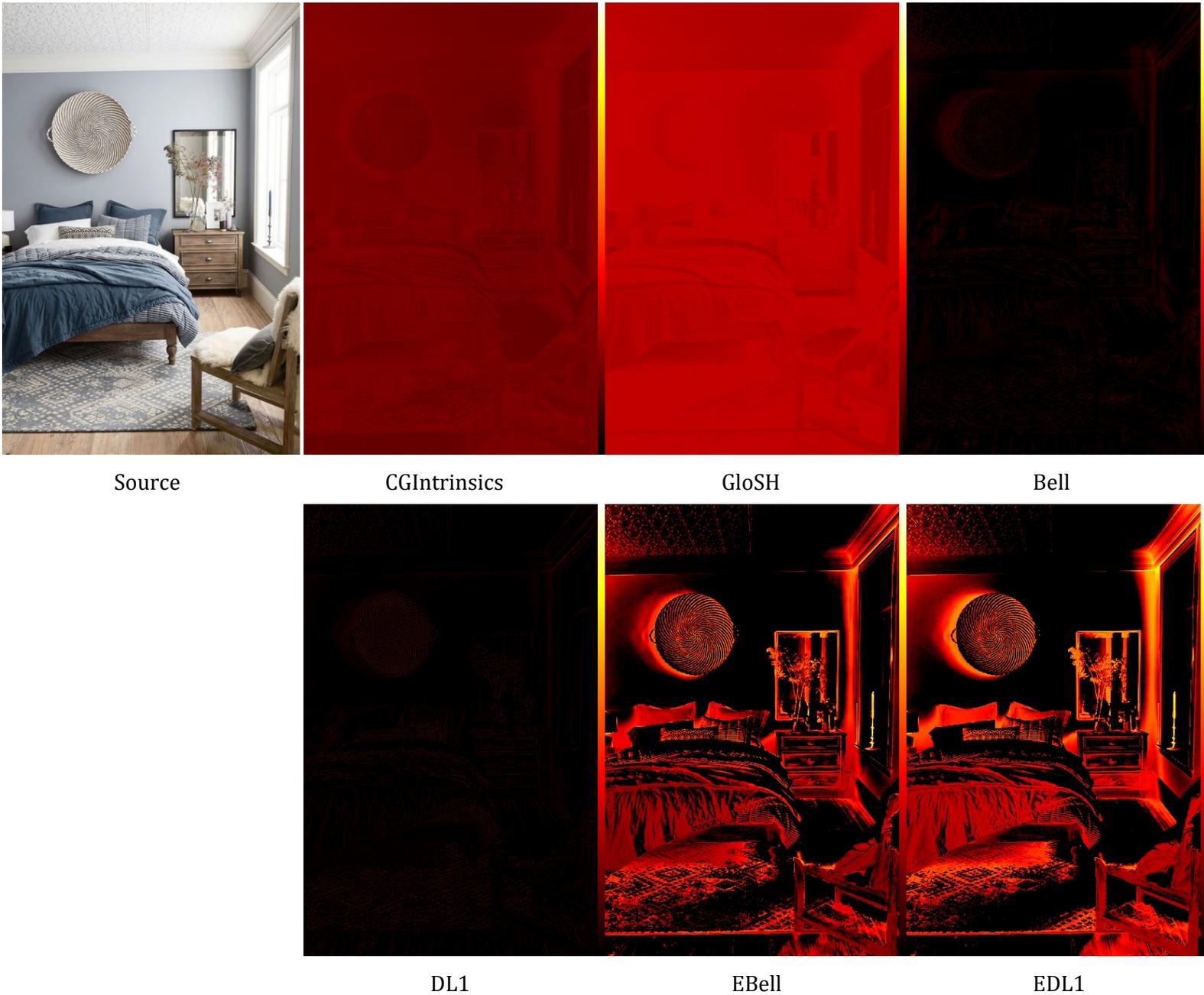


DL1

NBell

NDL1

Figure 53: **Shadow enhancement.** Visual comparison of shadow enhancement using different intrinsic decomposition methods.



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EBell

EDL1

Figure 54: **Shadow enhancement.** Log-distance map between shadow enhancement map and naive gamma correction map. This distance is computed as the log-space distance  $D_{\text{distance}} = \log Y_{\text{enhanced}} - \log X^k$  with  $Y_{\text{enhanced}}$  being the shadow-enhanced map and  $X^k$  is the k-gamma-corrected image ( $k = 2.0$ ). This distance reflects to what extent the enhanced shadows are meaningful and different from the naive gamma corrections. Working in log space prevents zero division and yields results faithful to the irradiance models in previous intrinsic literature. We visualize the negative part (or called the shadow part) of this measurement.



Source



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Figure 55: **Shadow enhancement.** Visual comparison of shadow enhancement using different intrinsic decomposition methods.

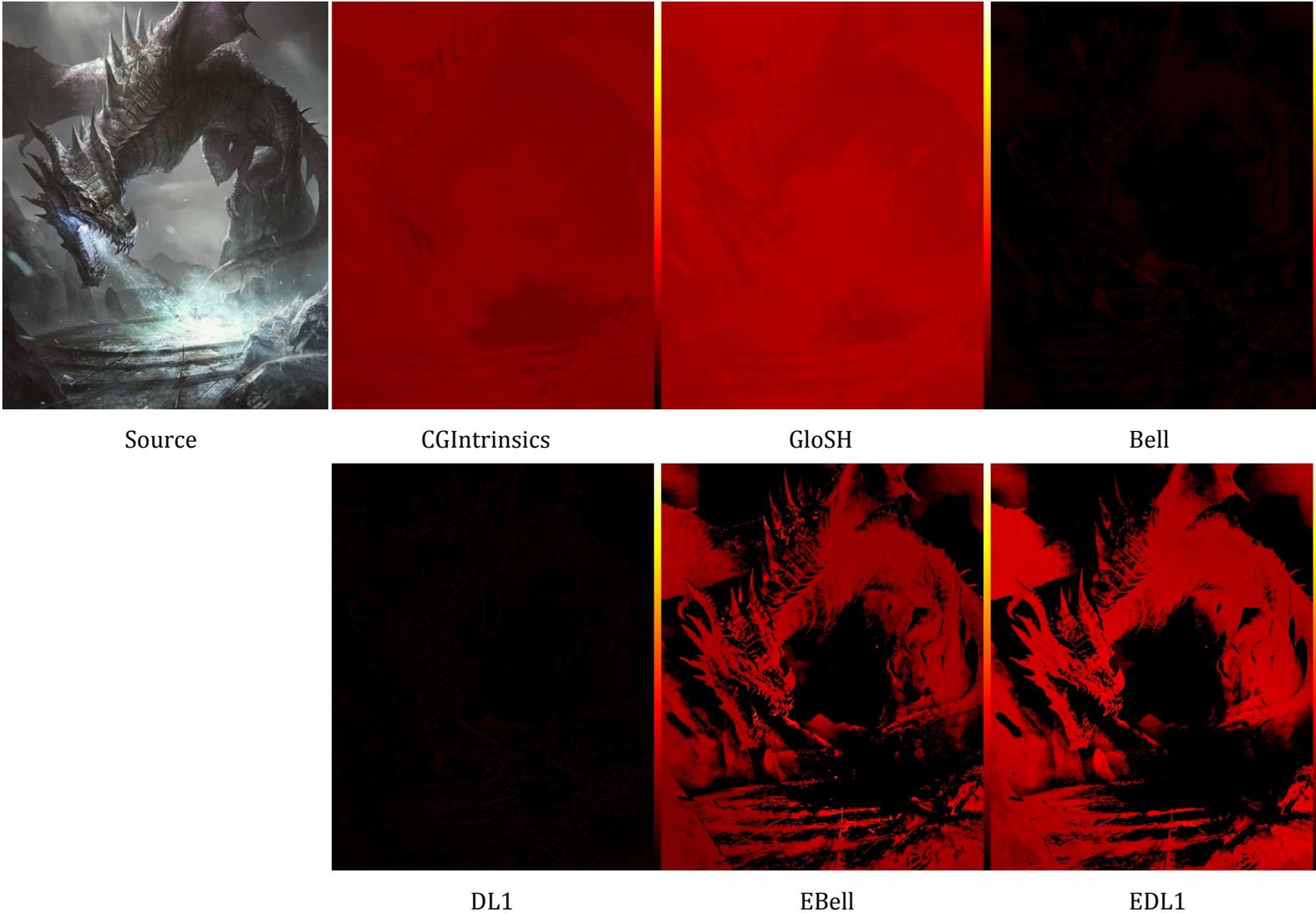


Figure 56: **Shadow enhancement.** Log-distance map between shadow enhancement map and naive gamma correction map. This distance is computed as the log-space distance  $D_{\text{distance}} = \log Y_{\text{enhanced}} - \log X^k$  with  $Y_{\text{enhanced}}$  being the shadow-enhanced map and  $X^k$  is the  $k$ -gamma-corrected image ( $k = 2.0$ ). This distance reflects to what extent the enhanced shadows are meaningful and different from the naive gamma corrections. Working in log space prevents zero division and yields results faithful to the irradiance models in previous intrinsic literature. We visualize the negative part (or called the shadow part) of this measurement.

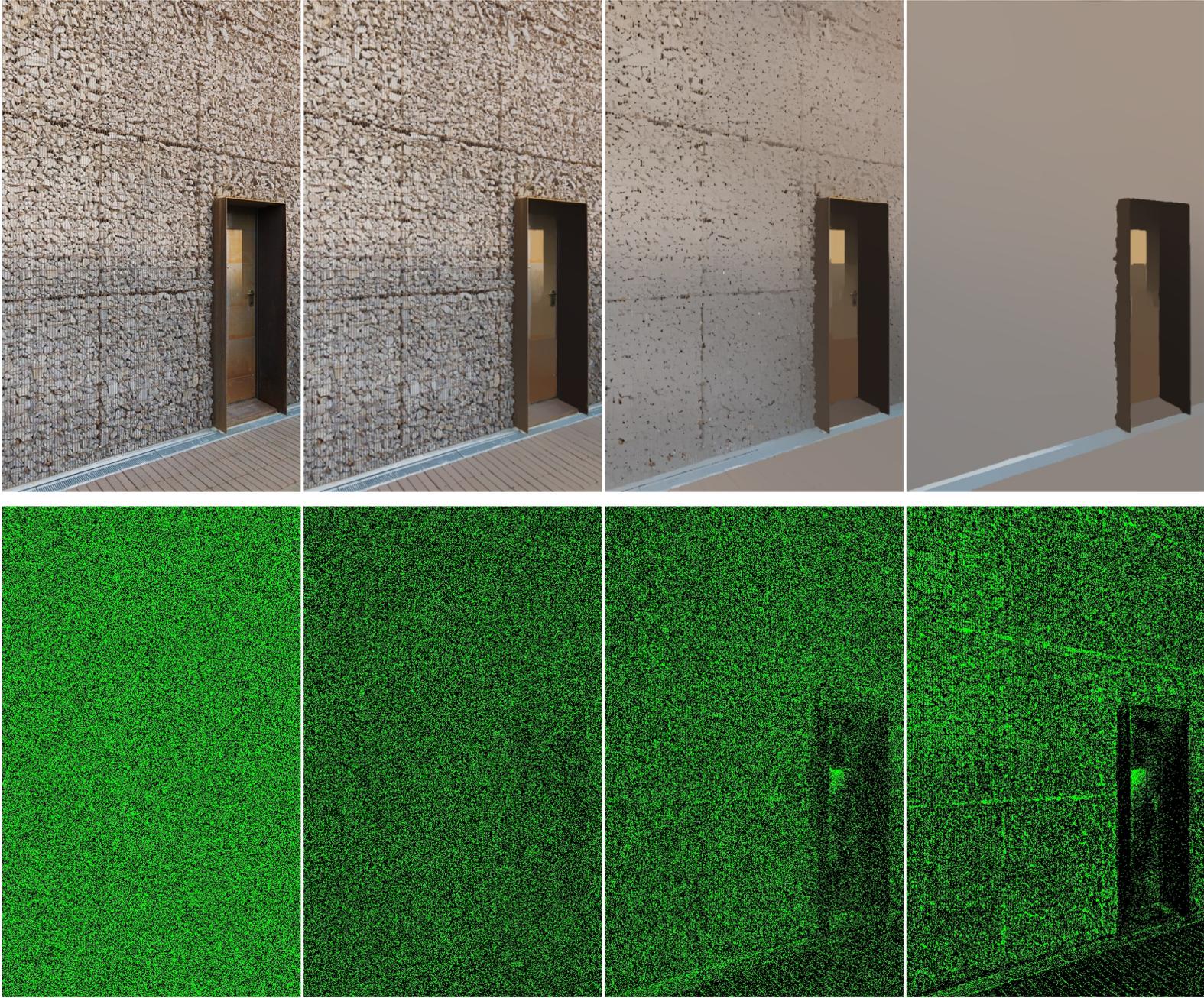


Figure 57: **Erasing position visualization.** Extended  $\mathcal{E}$  visualization as in the main paper. In the first row are the smoothed results using EDL1 at iteration 0, 1, 3, and 7. In the second row is the visualized erasing sets  $\mathcal{E}$ , marked in green. Please refer to main article for expositions.

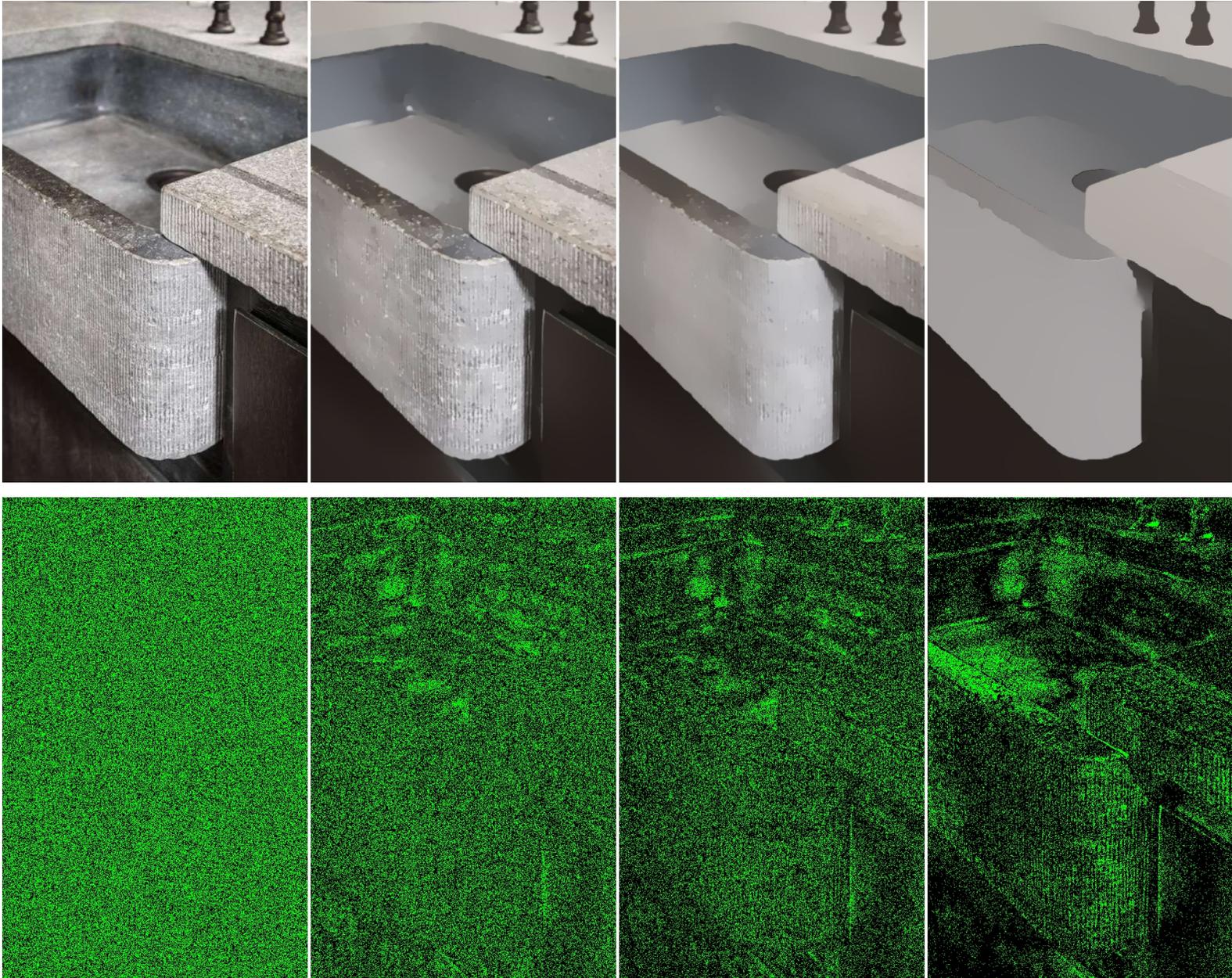


Figure 58: **Erasing position visualization.** Extended  $\mathcal{E}$  visualization as in the main paper. In the first row are the smoothed results using EDL1 at iteration 0, 1, 3, and 7. In the second row is the visualized erasing sets  $\mathcal{E}$ , marked in green. Please refer to main article for expositions.

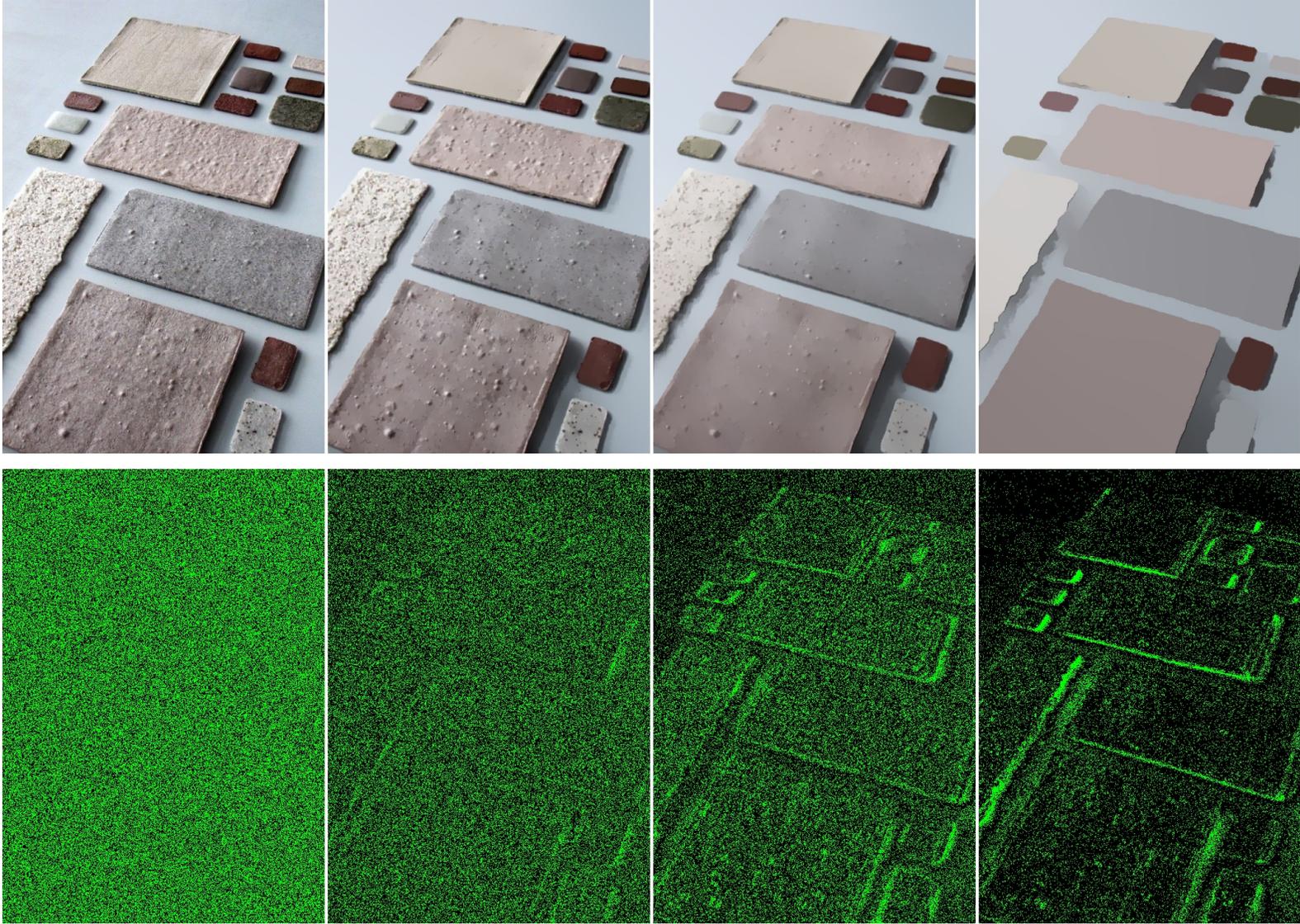


Figure 59: **Erasing position visualization.** Extended  $\mathcal{E}$  visualization as in the main paper. In the first row are the smoothed results using EDL1 at iteration 0, 1, 3, and 7. In the second row is the visualized erasing sets  $\mathcal{E}$ , marked in green. Please refer to main article for expositions.

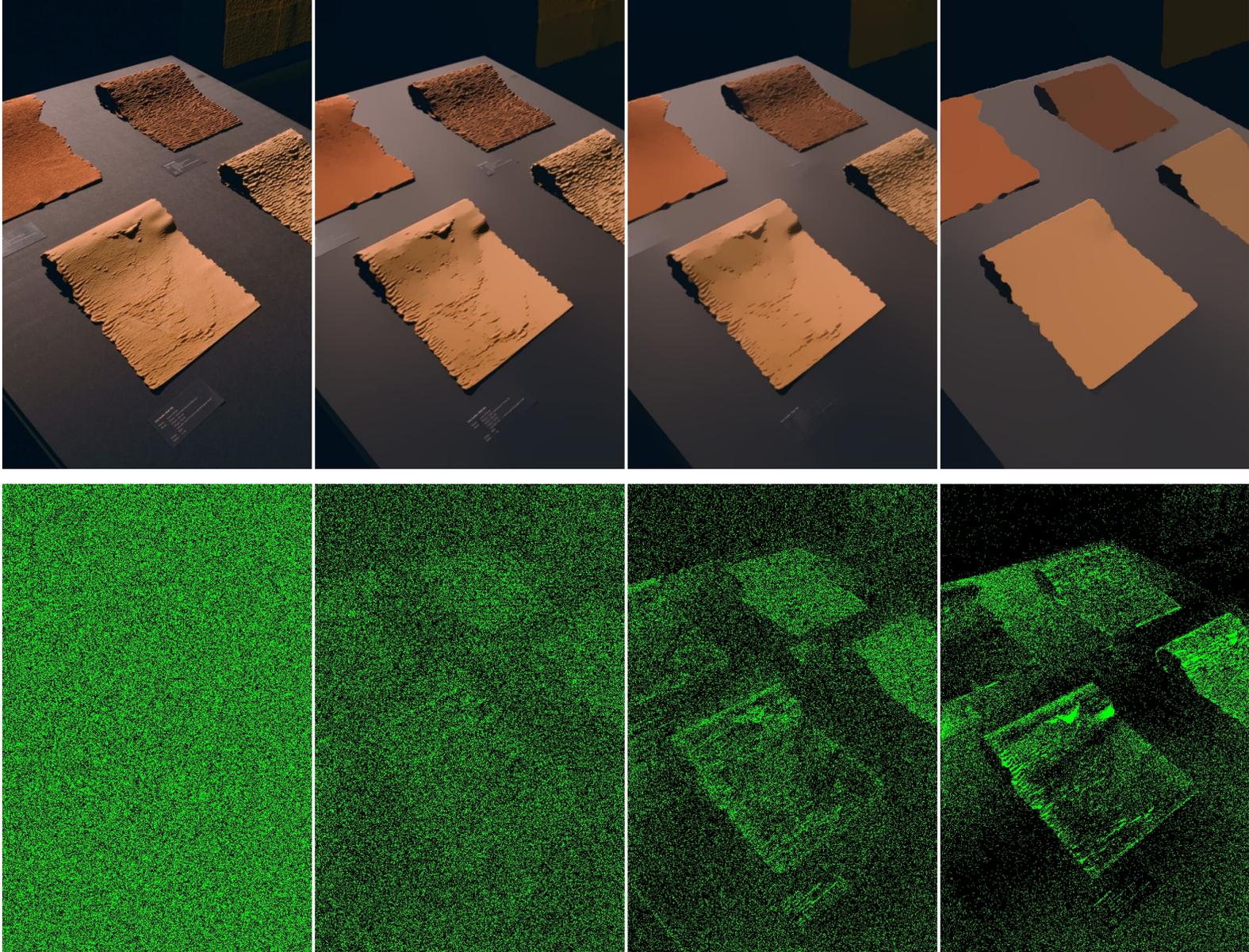


Figure 60: **Erasing position visualization.** Extended  $\mathcal{E}$  visualization as in the main paper. In the first row are the smoothed results using EDL1 at iteration 0, 1, 3, and 7. In the second row is the visualized erasing sets  $\mathcal{E}$ , marked in green. Please refer to main article for expositions.

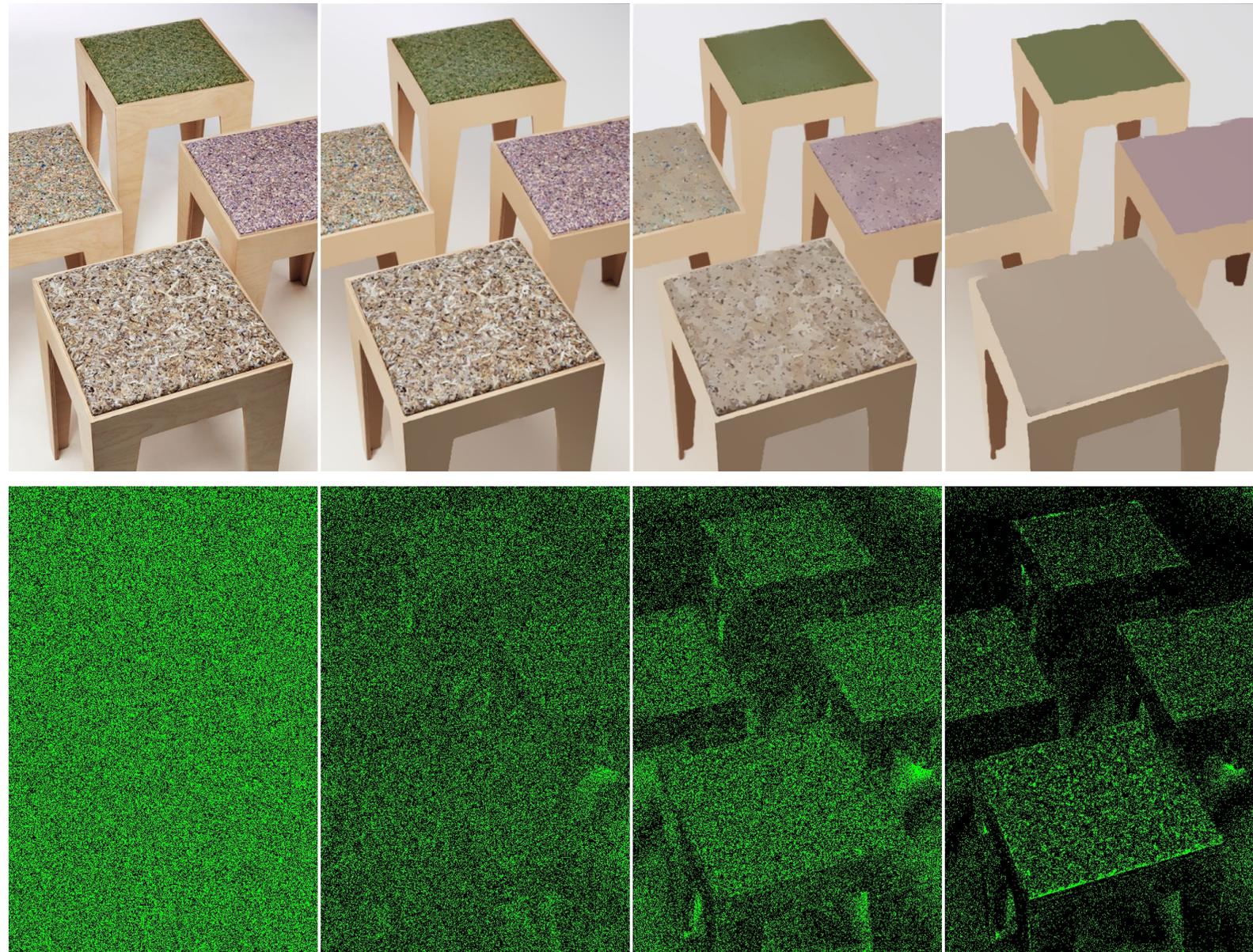


Figure 61: **Erasing position visualization.** Extended  $\mathcal{E}$  visualization as in the main paper. In the first row are the smoothed results using EDL1 at iteration 0, 1, 3, and 7. In the second row is the visualized erasing sets  $\mathcal{E}$ , marked in green. Please refer to main article for expositions.

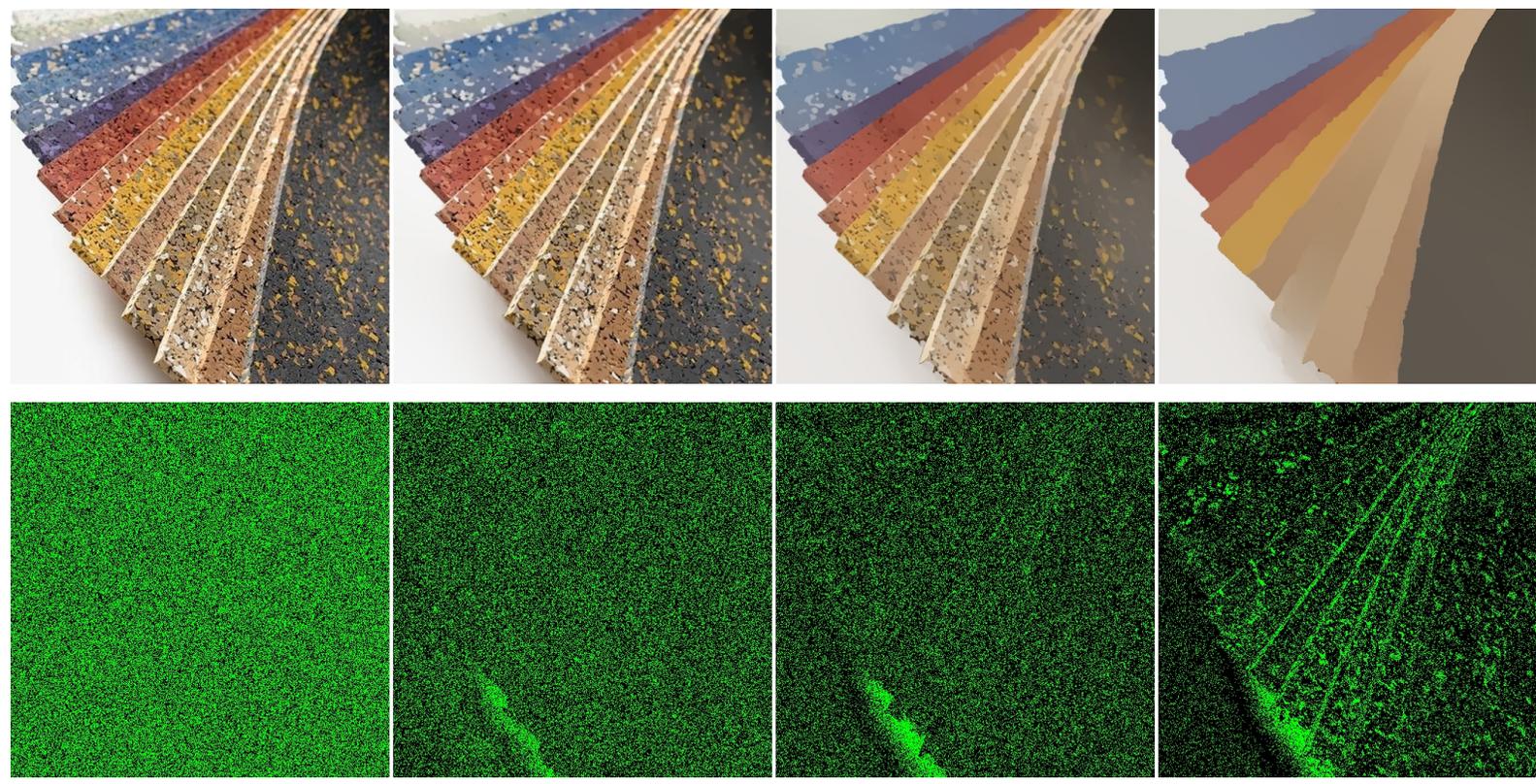


Figure 62: **Erasing position visualization.** Extended  $\mathcal{E}$  visualization as in the main paper. In the first row are the smoothed results using EDL1 at iteration 0, 1, 3, and 7. In the second row is the visualized erasing sets  $\mathcal{E}$ , marked in green. Please refer to main article for expositions.



Source

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DL1

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EDL1

Figure 63: **Limitation.** The specular reflection removal causes unrealistic result in this example.